Articular contact vs. embedding: Effect of simplified boundary conditions on the stress distribution in the distal radius and volar plate implant loading

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Abstract:

Boundary conditions (BCs) are often simplified in experimental and numerical models simulating distal radius fractures and their treatments. The aim of this study was to investigate the effects of simplified BCs at the radiocarpal joint: (1) on the stress distribution in the intact distal radius, and (2) on the loading of a volar locking plate (VLP) used for distal radius fracture treatment. Finite element models of the distal radius with contact between the carpals and the cartilage were created as reference models for an intact bone and a fractured bone with VLP treatment. Four models with simplified BCs were compared to these reference models: One with embedding material instead of carpals, one with carpals tied to the radius; each loaded either uniaxially or with statically equivalent loading to the reference model. Differences in distal bone stress distributions and mechanical parameters of the VLP (fracture gap motion, plate peak stresses, distal screw loads) were generally largest for the uniaxially loaded, embedded model (up to 250% in individual screw loads) and smallest for the model with tied carpals and statically equivalent loads (<25% for all parameters). Differences were greatly reduced if statically equivalent loads were applied, but subchondral stress peaks were absent without carpals. Thus, realistic multiaxial loading seems to be most important when modelling the mechanical behavior of the distal radius and fracture treatments. Carpals should be included at least with tied contact to the radius if subchondral bone stresses or individual screw loads of a VLP are investigated.

1. Introduction

 Distal radius fractures (DRFs) are among the most common fractures (Nellans et al., 2012). A frequent type of DRF is the Colles' fracture, for which the fracture location lies just 2-3cm proximal from the radio- carpal joint (RCJ) (Baumbach et al., 2011). If the DRF is unstable, treatment typically involves surgical re-duction and internal fixation using a volar locking plate (VLP) (Sander et al., 2020).

 In the past, finite element (FE) models have been extensively used to investigate DRF mechanics(Edwards and Troy, 2012; Varga et al., 2009) and mechanical parameters after fracture treatment (Knežević et al., 2017; Yamazaki et al., 2021), such as fracture gap movement (FGM) (Caiti et al., 2019; Liu et al., 2020). Still, boundary conditions (BCs) are often highly simplified in these models, which might limit their clinical relevance. For instance, some models simulated uniaxial compression with load application through em- bedding materials (Synek et al., 2015; Varga et al., 2009) or simply applied the load directly at the articular surface (Caiti et al., 2019; Liu et al., 2020). Only a few included the carpals with contact conditions or at least tied to the radius cartilage (Edwards and Troy, 2012; Pistoia et al., 2002).

 Simplifications of BCs are based on the idea that stress distribution differences will decrease quickly with increasing distance from the point of load application, if statically equivalent loads are applied (Saint- Venant, 1855). However, the stresses of interest in the distal radius are close to the point of load applica- tion. It is yet unknown to what extent simplifications of BCs influence the stress distributions in the sub- chondral and Colles' fracture region of the radius and how this error propagates to VLP loading and FGM. The goal of this study was to systematically investigate the effect of simplified BCs (1) on the stress distri- bution in the intact distal radius and (2) on the mechanical parameters of a fractured distal radius with VLP treatment. To achieve this goal, FE models with contact interaction at the RCJ are established as ref- erence models (RMs) and compared to models with simplified BCs using embedding material or tied con-tact interaction.

2. Methods

2.1. Intact Bone Reference Model

 A computed tomography (CT) scan (male, 53 years, 1.69m, 79kg) from the medical image repository of the Swiss Institute for Computer Assisted Surgery (https://www.smir.ch) (Swiss Institute for Computer Assisted Surgery, 2020) with a voxel size of 1.27x1.27x0.25mm was rescaled to an isotropic resolution of 0.25x0.25x0.25mm and used to segment cortical and trabecular regions and carpals using 3DSlicer (https://www.slicer.org/) (Kikinis et al., 2014). Geometrical model adaptations were performed using Au- todesk Fusion 360 (Autodesk, Inc., San Rafael, CA, USA), and the FE model was created in Abaqus 2020 (Dassault Systèmes, Vélizy-Villacoublay, FRA). The coordinate system was defined following the recom- mendations of the international society of biomechanics (Wu et al., 2005). The bone was cut to a length of 100mm from the tip of the radial styloid process. The articular cartilage was created as a 1mm layer (Pollock et al., 2013) on the distal end of the radius (Figure 1) and connected to the radius using a tie constraint.

 Radius and cartilage were meshed with quadratic tetrahedral elements, while carpals were meshed with shell elements. A mesh convergence analysis resulted in an average element size of 1.5mm (see Appen- dix). Trabecular and cortical regions were modelled as isotropic homogeneous elastic materials(*E*=1.4GPa and *E*=17GPa, respectively with *ν*=0.3) (Synek et al., 2015) and the cartilage as a hyperelastic neo-Hookean material with *E*=10MPa and *ν*=0.45 (Armstrong et al., 1984). The carpals were modelled as a single rigid body. All degrees of freedom were locked at the proximal end of the radius, and only displacement in longitudinal direction was unconstrained for the carpals (Figure 1). A force of 250N was applied on the carpals through a reference point, based on previous estimations of physiological loading in the RCJ (Christen et al., 2013). Contact interaction was modelled between the carpals and the cartilage using a surface-to-surface discretization method with a finite-sliding formulation. Contact was enforced using the augmented Lagrange multiplier method with a hard pressure-overclosure relationship and frictionless be-

Figure 1: (a) Reference models of both the intact distal radius and the fractured radius with a VLP implant and (b) simplified boundary conditions. Simplified models include the embedded models (EM) and models with tied carpals (TM), each loaded uniaxially (EMu, TMu) or multiaxially with load statically equivalent to the reference models (EMm, TMm; statically equivalent loads highlighted in red). Points A and B used for fracture gap movement (FGM) calculation.

2.2. Fractured Bone Reference Model

 Models with simplified BCs involved one model loaded using an embedding rather than carpals (EM) and one model loaded via the carpals connected with a tie constraint to the cartilage (TM) (Figure 1). The embedding was modelled as a polyurethane (*E*=1.45GPa and *ν*=0.3) (Synek et al., 2015) cylinder with di- ameter of 50mm connected to the radius and cartilage using a tie constraint. Load magnitude and BCs were identical to the RM. For the TM, the cartilage was extruded to the proximal surface of the carpals. 65 These two models were referred to as uniaxial loaded models EM_u and TM_u . Furthermore, statically equiv- alent loads to the RM were applied to both simplified models. Therefore, the necessary forces and mo- ments to be applied at the reference node were calculated based on static equilibrium equations. These 68 two models were referred to as multiaxially loaded models EM_m and TM_m (Figure 1).

2.4. Evaluation of differences

 The stress distribution between the intact bone RM and the simplified models were compared ele- mentwise since the models shared the same bone mesh topology. The effective stress *σ*̅, defined as *σ*̅=√2*EU*, where *E* is the Young's modulus and *U* the strain energy density, was used as an equivalent stress variable. The error was evaluated as the root mean square error, normalized by the mean stress (NRMSE) in different regions. First, the NRMSE was computed in 1mm slices from distal to proximal throughout the 75 entire bone (NRMSE_{Slice}). Second, the NRMSE was evaluated for the entire subchondral and Colles' fracture 76 region (NRMSE_{Region}). The Colles' fracture region was defined at 22 \pm 4mm proximal from the tip of the radial styloid process (Eastell et al., 1989). Cortical and trabecular regions were analyzed separately.

 For the fractured bone models with VLP treatment, stresses in the distal fracture fragment were analyzed in analogy to the intact bone model. Three additional parameters were evaluated: 1) FGM, 2) peak von Mises stresses in the plate and 3) distal screw loads at the screw-plate interface. FGM was calculated as the change in distance between two nodes on the dorsal side of the radius on either side of the fracture 82 gap (Figure 1). Peak von Mises stresses in the plate (σ_{vM,peak}) were evaluated as the 99th percentile to 83 exclude outliers. Screw forces and moments were split into axial force (F_{axial}), shear force (F_{shear}) and the 84 total moment (M_{tot}) .

85 **3. Results**

86 *3.1. Intact bone models*

87 Qualitative comparison of stress distributions showed that increased complexity of BCs resulted in pro-88 nounced stress peaks in the subchondral region (Figure 2). If statically equivalent loads were applied, the 89 error in the embedded model could be reduced considerably, although stress peaks close to the joint were 90 still missing. Quantitative model comparison (Figure 3) revealed that the NRMSE_{Region} was largest for the 91 EM_u in the subchondral trabecular region (133%) and smallest for the TM_m in the cortex of the Colles' 92 fracture region (5%). Furthermore, NRMSE_{Region} was overall larger in the subchondral region compared 93 the Colles' fracture region for all simplified models.

Figure 2: Contour plots of the effective stress (σ̅*) of the intact bone models in ascending order of complexity regarding their boundary conditions. Vertical white lines distinguish the subchondral from the Colles' fracture region.*

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Figure 3: (a) Normalized root mean square error (NRMSESlice) of the effective stress (σ̅*) along the bone between the reference model (RM) and the simplified models (EMu, EMm, TM^u and TMm) for cortex and trabecular region. (b) NRMSE of the subchondral and trabecular regions (NRMSERegion) displayed as a colormap representation of the bone sections.*

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97 *3.2. Fractured bone models*

98 Qualitatively, the fractured bone model with VLP showed less pronounced stress peaks in the subchondral

99 bone for the embedded models (Figure 4). Still, using statically equivalent loading reduced the error of

100 the embedded model considerably. Quantitatively, largest differences were observed for the EMu and 101 smallest for the TM_m (Figure 5). Differences in the uniaxially loaded models were larger than 50% for FGM 102 and peak plate stress and reached up to 250% for individual screw loads in the EM_u. Using statically equiv-103 alent loading (EM_m), relative differences decreased to less than 30% for the screw loads and less than 6% 104 for FGM and peak plate stresses. If carpals were additionally included (TM_m), the error further decreased 105 to below 10% for all parameters.

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Figure 4: Contour plots of the effective stress ($\bar{\sigma}$) of the bone as well as von Mises stress (σ _{VM}) of the volar *locking plate (VLP) of the reference model (RM) and simplified models (EMu, EMm, TM^u and TMm) in ascending order of complexity regarding their boundary conditions.*

Figure 5: Colormap plots of the relative differences in fracture gap movement (FGM), VLP peak stress (σvM,peak), axial screw force (Faxial), shear screw force (Fshear) and total screw moment (Mtot) and regional normalized root mean square error (NRMSERegion) of the fracture fragment of the radius. Values of differences are presented for each condition in grey boxes or on top of the respective screws.

4. Discussion

- Overall, the results showed that simplified BCs at the RCJ can affect both the stress distribution in the
- distal radius and the simulation outcomes of the fractured radius with VLP treatment.
- 113 In the intact distal radius, stresses in the Colles' fracture region were generally less affected by simplified
- BCs compared to subchondral bone stresses. However, using uniaxial loading instead of statically equiva-
- lent loadsin the embedded models still led to considerable errors in the Colles' fracture region. This result
- is in line with Johnson and Troy (2018), who reported differences of the load distribution in the fracture

 region between physiological and uniaxial loading at the RCJ. In addition to their study, our results indicate that carpals do not necessarily need to be included for realistic stress distributions in the fracture region if realistic multiaxial loading is applied. This is supported by Varga et al. (2009), who were able to repro- duce Colles' fractures in radii using embedding material rather than carpals, but tilted the bone for a more realistic load direction. Additional inclusion of carpals might only be relevant if subchondral bone stresses are investigated. In that case, using tie constraints rather than actual contact led to an acceptable average error (<25%). This also supports the use of simple voxel-based FE models with tied carpals (e.g. Pistoia et al. 2002), rather than creating complex models with smooth surfaces necessary to implement contact interaction.

 For the fractured distal radius with VLP treatment, the results were largely consistent with those of the intact bone. Realistic multiaxial loading proved to be of utmost importance for VLP parameters typically assessed in biomechanical studies such as peak implant plate loading and FGM (Caiti et al., 2019). How- ever, caution is warranted if the distribution of loads between screws is investigated, e.g. when comparing screw configurations (e.g. Drobetz et al., 2013), or if peri-implant bone loading is evaluated (e.g. Synek et al., 2021). To provide clinically more realistic results, these models should incorporate load introduction through carpals. As for the intact bone, the contact interaction might be replaced with tie constraints if realistic multiaxial loading is applied, without introducing substantial errors (<10%).

 Some limitations of this study must be mentioned. First, no experimental validation was performed. Ex- perimental assessment of stress distributions inside the bone was considered beyond the scope of this paper, as even measuring intraarticular pressure is challenging (Rikli et al., 2007). Second, the BCs in the RMs were still highly simplified. In particular, the carpals were fused, only axial translation was uncon- strained, and just one load magnitude was investigated. Still, these loading conditions allowed for system- atic comparison of different BCs as well as delineation of effects caused by different resultant loads and local articular stress peaks. Finally, homogenous, isotropic material properties were used for cortical and

- trabecular bone regions rather than material mapping based on local bone density. This decision was
- made to include the heterogeneous nature of the distal radius (i.e., thin but stiff cortex and more compli-
- ant trabecular bone) despite the low resolution of the available CT scan.
- 144 In conclusion, this study suggests that realistic multiaxial loading is most relevant for accurate predictions
- of the stress distribution in the intact distal radius and mechanical parameters of VLP treatment. Addi-
- tional inclusion of carpals might only be relevant if subchondral bone stresses, peri-implant bone stresses
- or individual distal screw loads are investigated. Modelling contact interaction between carpals and radius
- might be replaced by tie constraints if realistic multiaxial loading is applied.

Conflict of Interest

The authors declare that there are no conflicts of interest.

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