

Development of a global model for zenith wet delays based on the random forest approach

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Introduction

- Tropospheric delay is a major error source in the analysis of space geodetic observations

High correlation between **residual delay** and other parameters of interest such as **station height** and receiver clock bias

Incorrect modeling of tropospheric (wet) delay →
 affects precision and accuracy of position solution
 causes mis-interpretation of geophysical signals such as
 crustal deformation, terrestrial water storage variations

- Performance of tropospheric delay modeling is significantly limited due to the **high dynamics** of the **wet portion** in the neutral atmosphere
- Several positioning and navigation tasks such as **real-time applications** do not have the benefit of post-processing analyses, necessitating the availability of **accurate a-priori estimates for ZWD**.

Introduction

Ray-tracing through NWMs \Rightarrow Require the knowledge of **vertical profiles of temperature and humidity**

Saastamoinen (1972) model

$$ZWD = \frac{0.002277 \cdot \left(\frac{1255}{T} + 0.05 \right) \cdot e_s}{1 - 0.00266 \cos(2\phi) - 2.8 \cdot 10^{-7} h_s}$$

\Rightarrow Unable to account for spatial and temporal variations in the relationship

Global empirical troposphere models such as GPT3

\Rightarrow Unable to capture **daily and complex variations** of meteorological parameters

RF-based ZWD model

$$ZWD_{RF} = \begin{cases} f_{\text{blind}}(\text{DOY}, \text{lat}, \text{lon}, h_{\text{ell}}) \\ f(\text{DOY}, \text{lat}, \text{lon}, h_{\text{ell}}, e_s, T_s) \end{cases}$$

How can we **improve ZWD prediction accuracy** if meteorological data are available at some stations?

Without meteorological data

Meteorological data are available



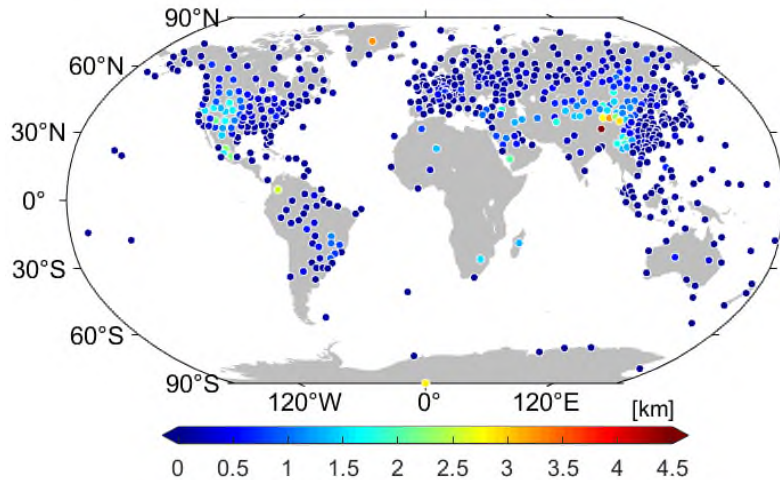
Dataset and Methodology

Radiosonde Measurements

Meteorological variables at discrete isobaric levels (usually twice per day)

Zenith wet delay (ZWD) are determined by the numerical integration of nonhydrostatic refractivity from the site's height to top sounding profiles

$$ZWD = 10^{-6} \int_{h_s}^{\text{top}} N_{nh} dh = 10^{-6} \int_{h_s}^{\text{top}} \left[\left(k_2 - \frac{R_d}{R_w} k_1 \right) \frac{P_w}{T} + k_3 \frac{P_w}{T^2} \right] \cdot Z_w^{-1} dh$$



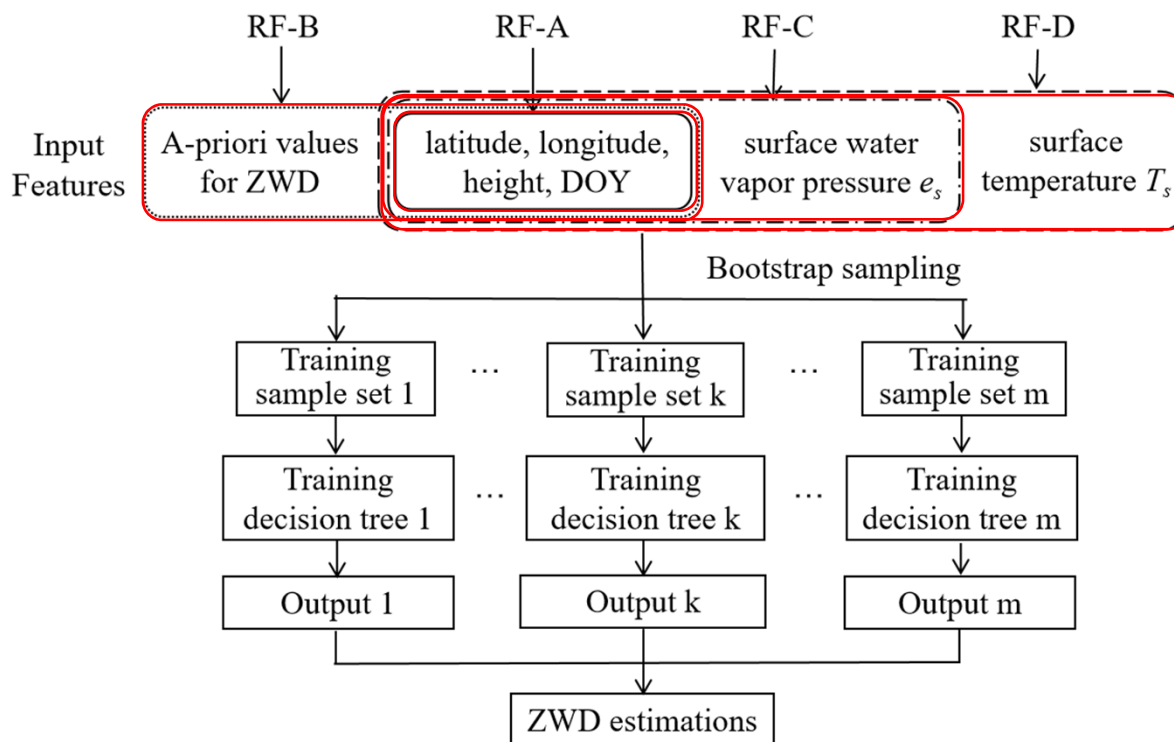
Modeling: 10 years (2010-2019) of radiosonde data at 586 sites

Validation: Sounding profiles for the year 2020

Dataset and Methodology

ZWD modeling based on the RF regression

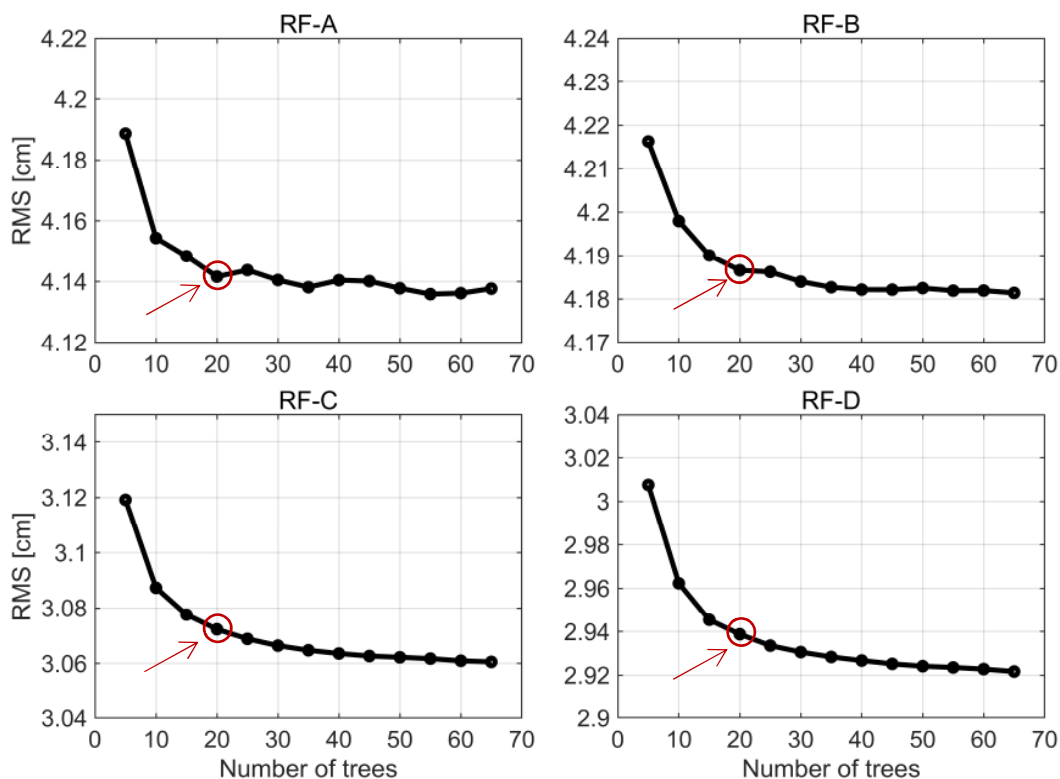
Functional formulation (RF-B): $ZWD_{RF-B} = f_u(\text{DOY}, \text{lat}, \text{lon}, \text{h}_{\text{ell}}, \text{ZWD}_{\text{priori}})$



Dataset and Methodology

Optional number of trees for a random forest system

10-fold **cross validation** RMS of ZWD differences between modeled and 'observed' values



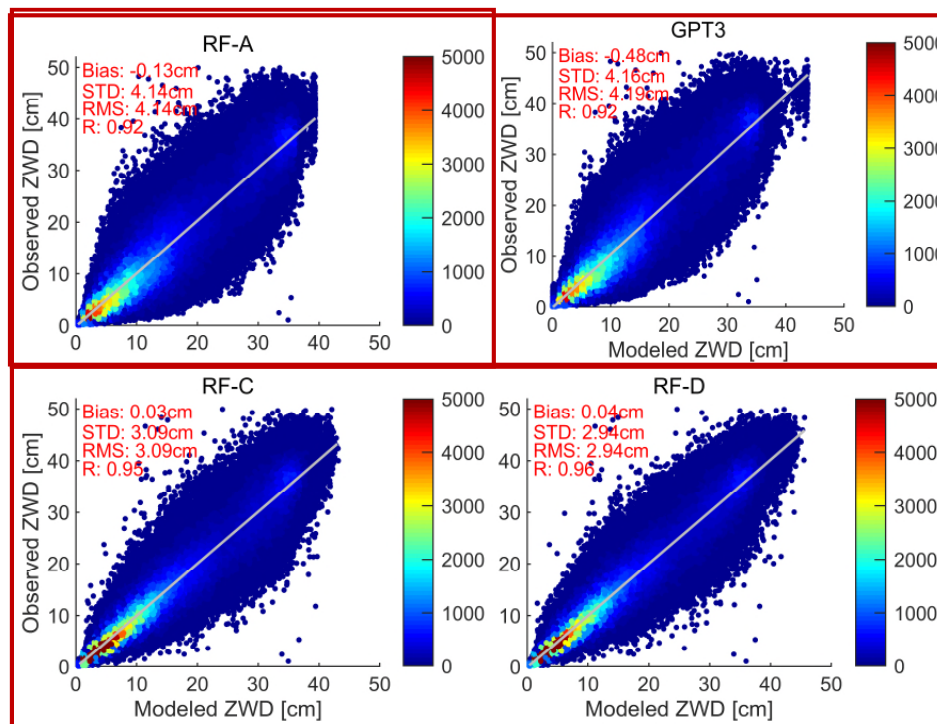
ZWD modeling accuracy tends to be stable when the **number of trees** is larger than **20**

Ensemble learning can help the RF-based ZWD model to achieve **better generalization ability**

Results

Overall performance of the RF-based ZWD models

ZWD prediction bias of 0.1 significantly improved by reduction of a priori surface topographic parameters in the functional formulation, especially for e_s



$$ZWD_{RF-A} = f_a(DOY, lat, lon, h_{ell})$$

$$ZWD_{RF-B} = f_b(DOY, lat, lon, h_{ell}, ZWD_{priori})$$

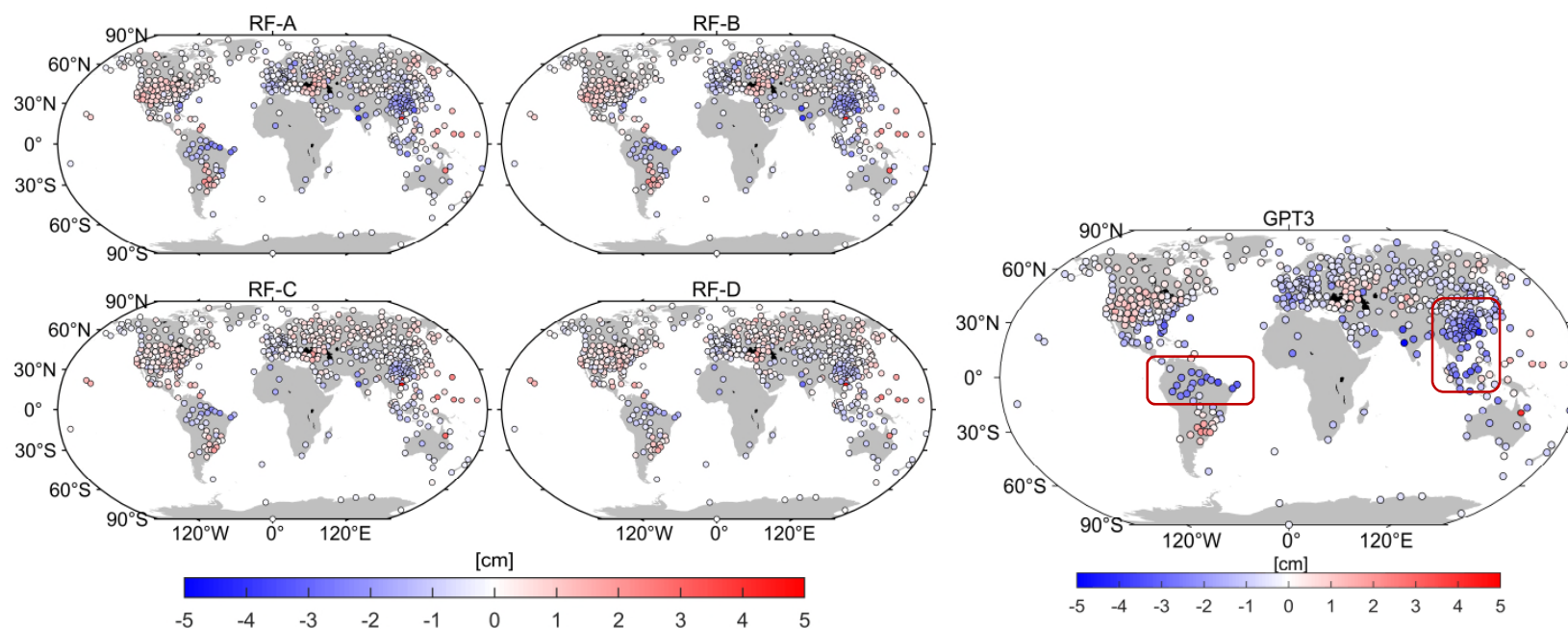
$$ZWD_{RF-D} = f_d(DOY, lat, lon, h_{ell}, e_s, T_s)$$

Model	Bias [cm]	STD [cm]	RMS [cm]	R
GPT3	-0.48	4.16	4.19	0.92
RF-A	-0.13	4.14	4.14	0.92
RF-B	-0.12	4.16	4.16	0.92
RF-C	0.03	3.09	3.09	0.95
RF-D	0.04	2.94	2.94	0.96

Results

Spatial features of model accuracy

RF-based ZWD models mitigate **negative biases** in the regions with **monsoon climate** and **tropical rainforest climate** types, in particular with the introduction of **surface meteorological information**

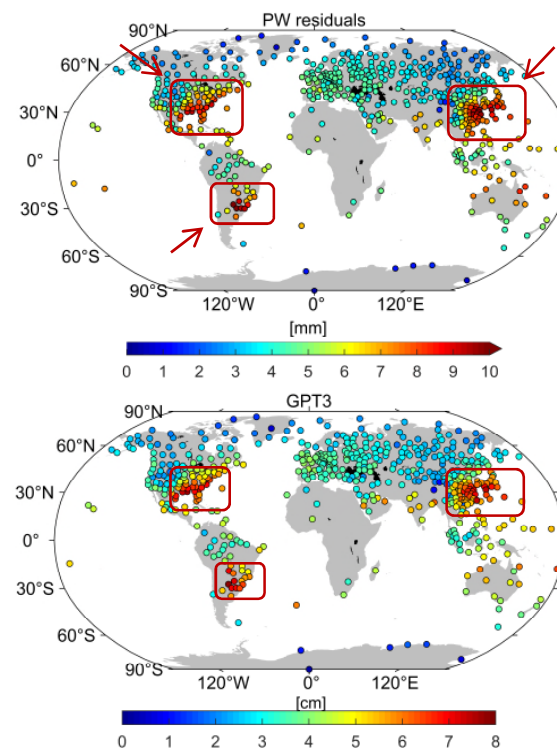
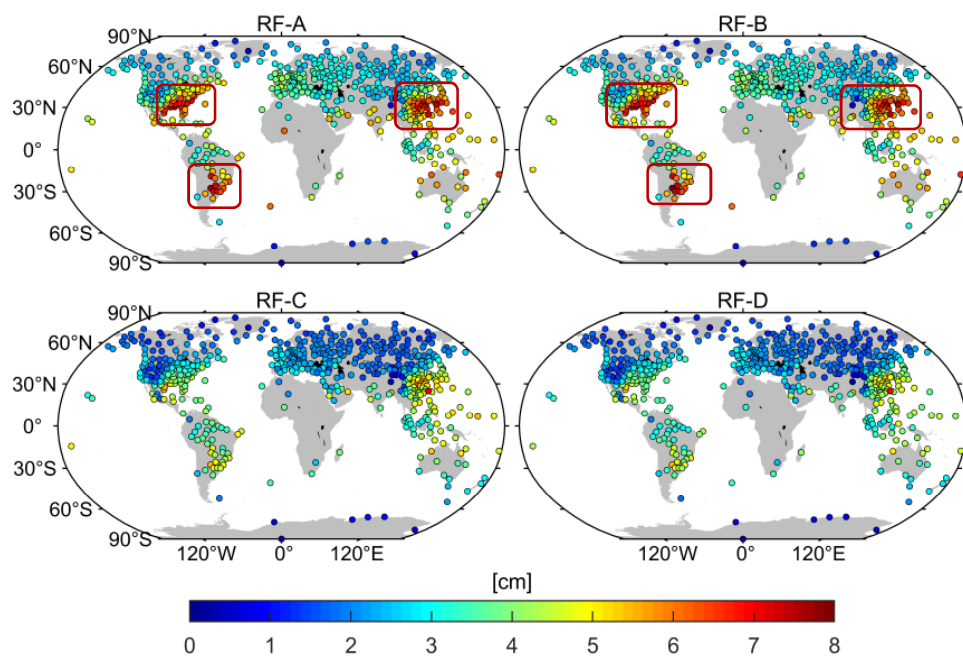


Results

Spatial features of model accuracy

Complex variations of the model accuracy in the low-latitude troposphere for the globe with missing climate meteorological parameters in the modeling

Mean values and seasonal components in PW time series were removed



- The RF-based ZWD model with meteorological parameterization (**RF-D**) can achieve an overall accuracy of **2.9 cm** and a bias close to zero
- ZWD modeling accuracy is **significantly improved** by the introduction of **surface water vapor pressure** into functional formulation in comparison with the **surface temperature**
- The RF-based ZWD models clearly mitigate **negative biases** in the regions with **monsoon climate** and **tropical rainforest climate** type
- Compared with the GPT3, ZWD modeling accuracy can be improved across the globe by considering **surface meteorological parameters**, especially in the regions with monsoon climate type

Thank you!

The subroutine of GZWD-RF model can be freely accessed from the VMF Data Server

https://vmf.geo.tuwien.ac.at/codes/gzwd_rf/

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