

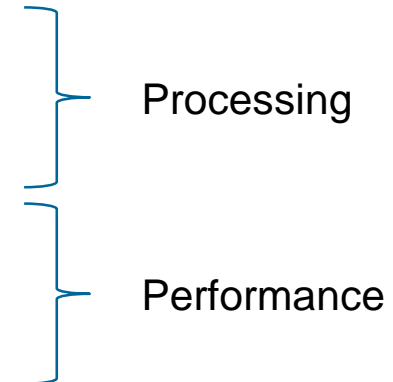
A series of six black satellite icons arranged in a curved path across the top of the slide. Each icon consists of a central square with two rectangular arms extending outwards.

PPP: PPP

Precise Point Positioning:
Processing, Performance and Potential

Outline

- GNSS fundamentals
- PPP theory
- High-quality data
- Low-cost data
- Potential

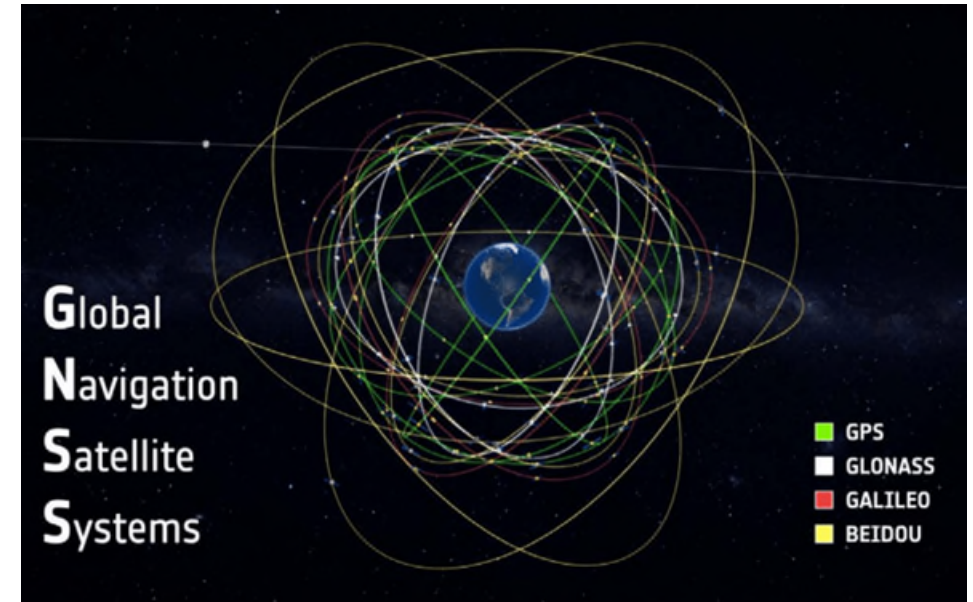


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GNSS

- Four major Global Navigation Satellite Systems:
GPS, GLONASS, Galileo, BeiDou
- Satellite constellations emitting signals
- Enable worldwide positioning and navigation service



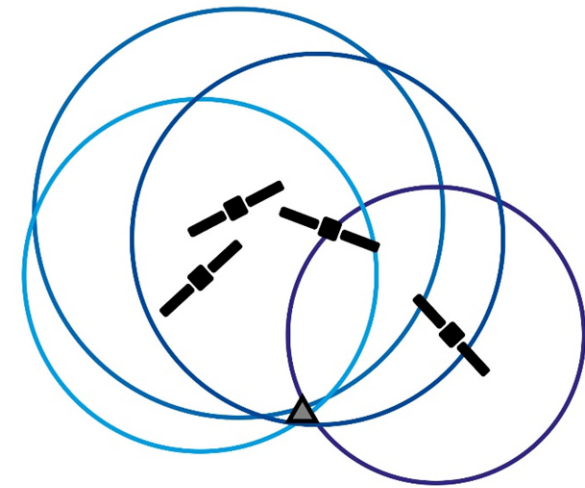
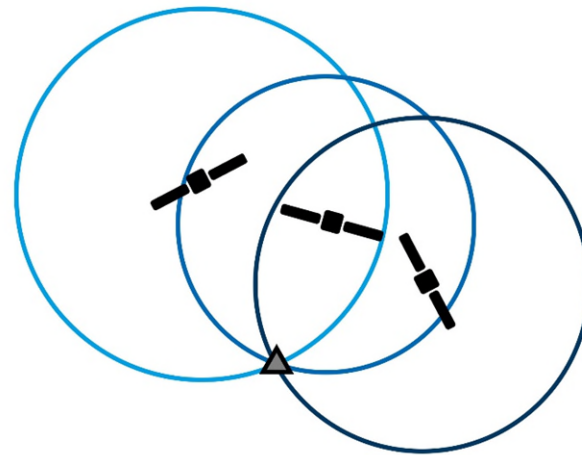
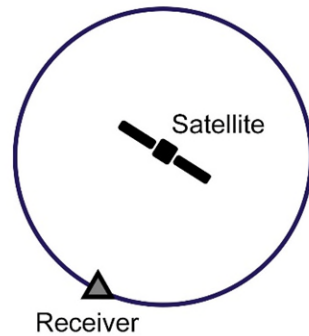
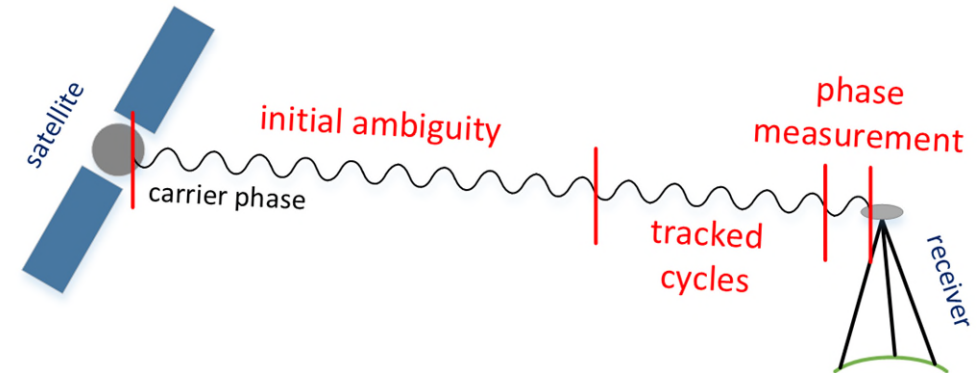
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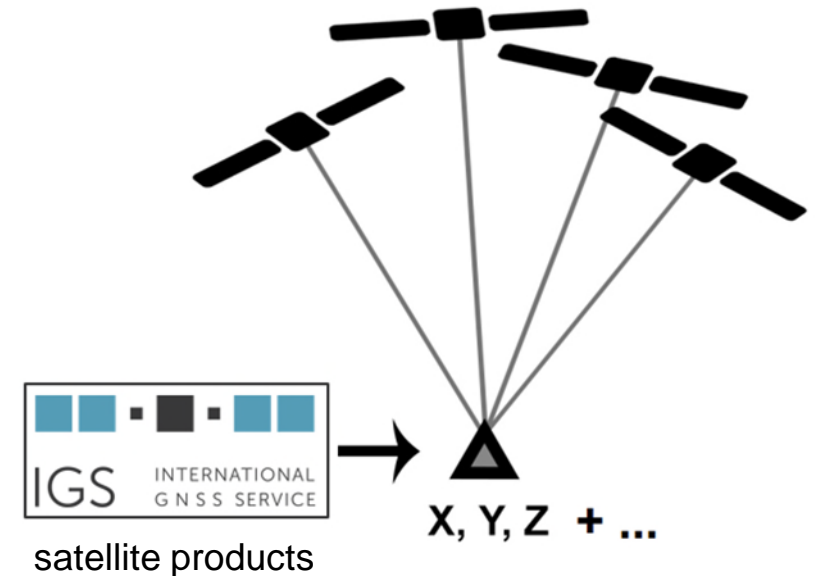
GNSS Positioning

- Code
- Phase
- Signal-to-Noise ratio
- Doppler



Precise Point Positioning

- PPP relies on precise satellite products: satellite orbits, clocks and biases
- Complex models and algorithms
- Position accuracy: cm, or even mm
- Major drawback: convergence time



multi-GNSS

multi-frequency

modern satellite
products

new PPP
models

**reduce
convergence time**

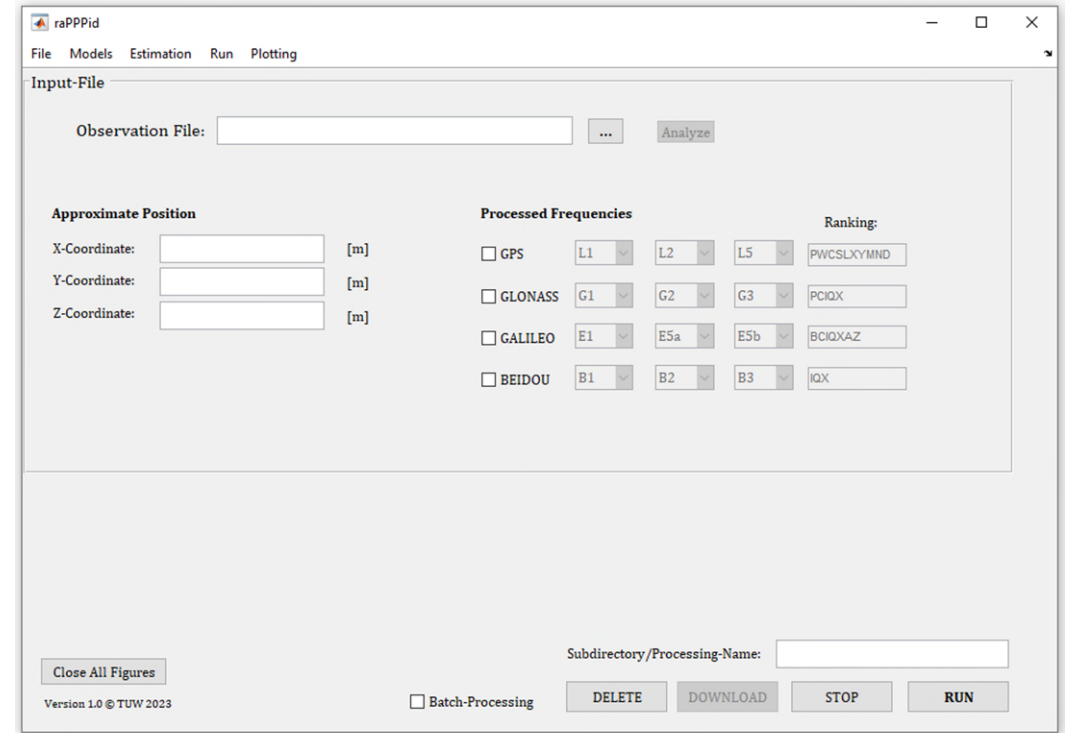
integer ambiguity
fixing

accurate error
models



raPPPid

- State-of-the-art PPP software
- Self-developed
- PPP module of VieVS
- GitHub:
<https://github.com/TUW-VieVS/raPPPid>
- Documentation:
<https://viewswiki.geo.tuwien.ac.at/en/raPPPid>

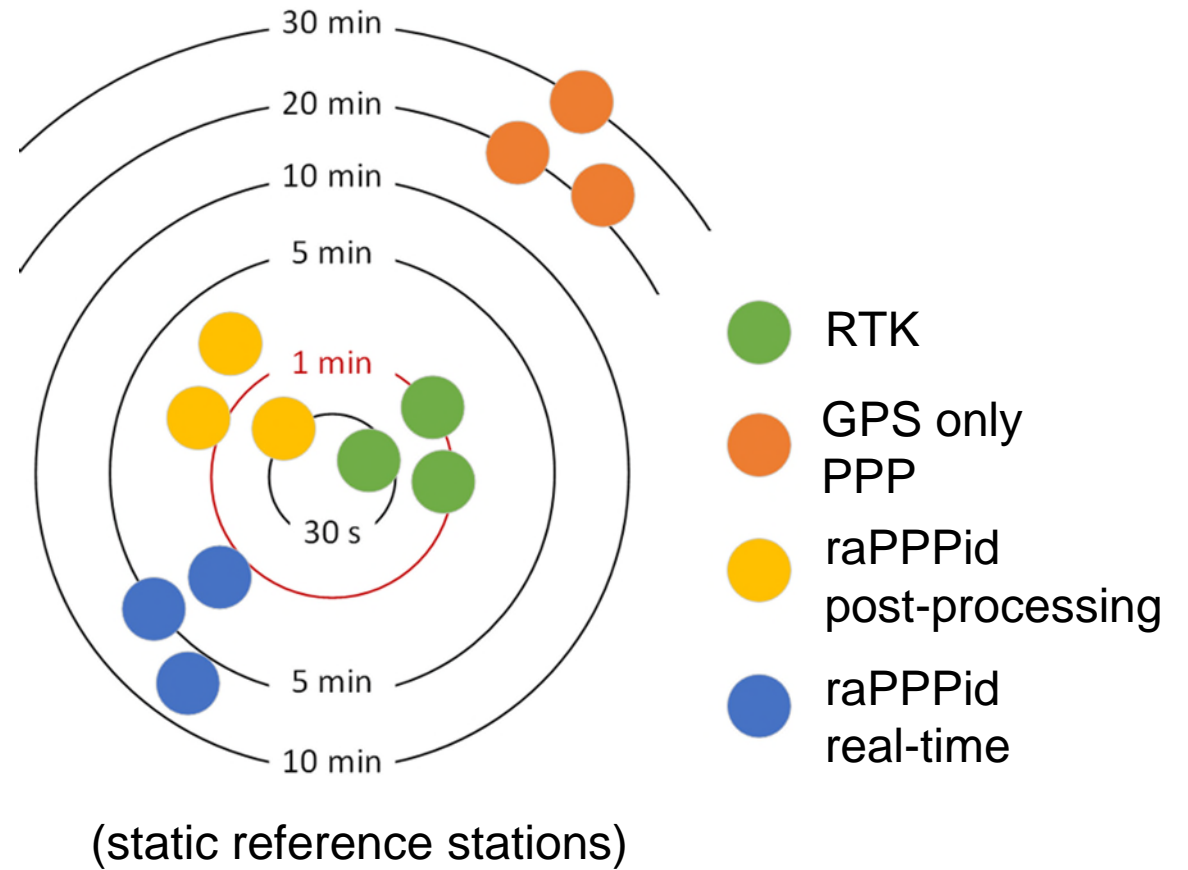


→ Convergence:

- Float (2D < 10 cm): several minutes
- Fixed (2D < 5 cm): 1 min or below

→ Accuracy: cm-level or below

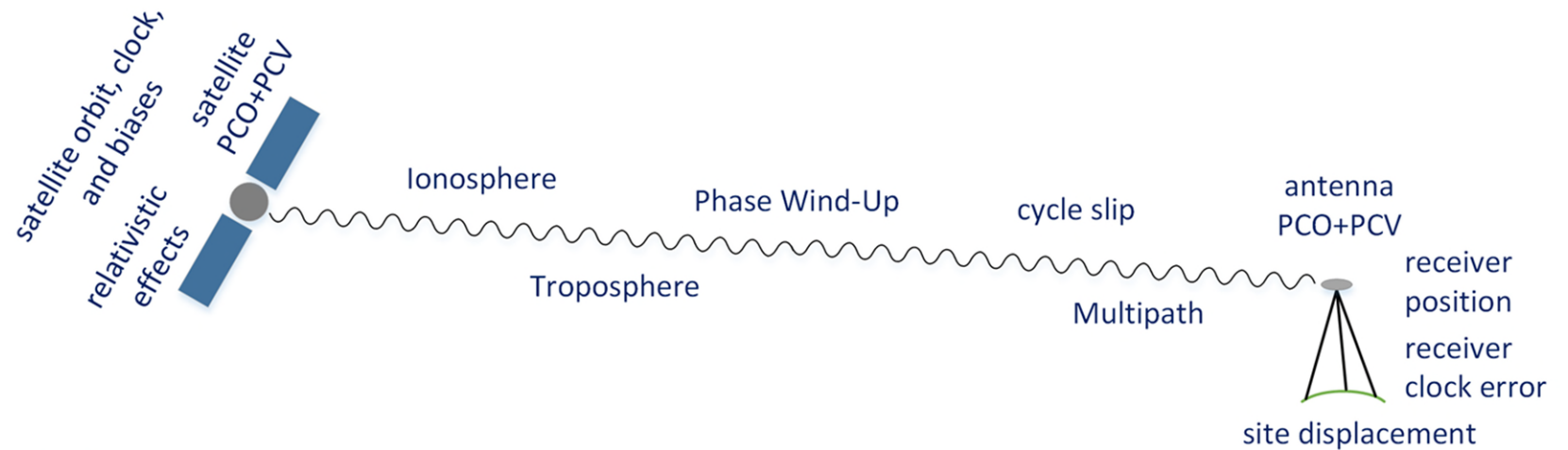
→ Comparable to RTK



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Error sources



$$L_i^{model} = \rho - c \cdot dt^S - dt_{rel} + c(dt_R^{GPS} + \delta t^g) - DCB_{1i}$$

$$- \frac{f_1^2}{f_i^2} \cdot dIono_1 + dTrop + dTrop_{residual}^{wet}$$

$$- \delta \rho_{solid} - \delta \rho_{oceanloading}$$

$$- \delta \rho_R^{PCO_i, PCV_i} + \delta \rho_R^{ARP_i} + \delta \rho_{PCO_i, PCV_i}^S$$

$$+ \delta \rho_{Wind-Up_i} + \lambda_i N_i$$

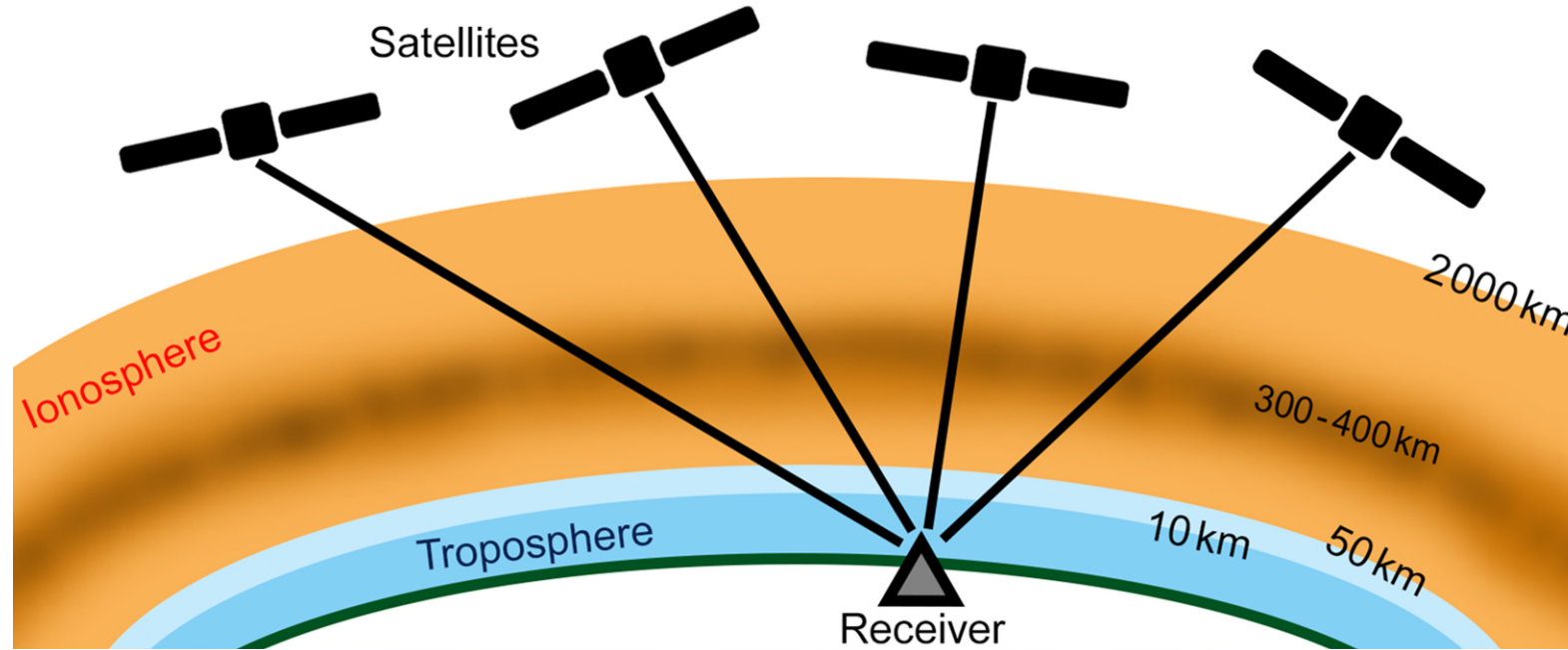
$$P_i^{model} = \rho - c \cdot dt^S - dt_{rel} + c(dt_R^{GPS} + \delta t^g) - DCB_{1i}$$

$$+ \frac{f_1^2}{f_i^2} \cdot dIono_1 + dTrop + dTrop_{residual}^{wet}$$

$$- \delta \rho_{solid} - \delta \rho_{oceanloading} + \delta \rho_{GDV_i}$$

$$- \delta \rho_R^{PCO_i, PCV_i} + \delta \rho_R^{ARP_i} + \delta \rho_{PCO_i, PCV_i}^S$$

→ many to consider



Ionospheric delay

- Major error source
- Strong fluctuations
- Challenging

Tropospheric delay

- Hydrostatic and wet part
- ~90% and ~10%
- Model and estimate

Error sources

Symbol	Description	Magnitude
ρ	Theoretical distance	10^7 m
dt^S	Satellite clock error	μs - ns
dt_{rel}	Relativistic effects	10 ns
dt_R^{GPS}	Receiver clock error	ns-ms
δt^g	Receiver offset GNSS	ns
$-DCB_{\Pi}$	Receiver DCB	ns
$dIono_1$	Ionospheric delay	1-20 m
$dTrop$	Tropospheric delay	1-15 m
$dTrop_{residual}^{wet}$	Residual wet delay	mm-dm
$\delta\rho_{solid}$	Solid Earth tides	cm
$\delta\rho_{GDV_i}$	Group Delay Variations	mm-1 m
$\delta\rho_{oceanloading}$	Ocean loading	mm-cm
$\delta\rho_{PCO_i,PCV_i}^S$	Satellite PCO and PCV	1 m, mm-cm
$\delta\rho_R^{PCO_i,PCV_i}$	Receiver PCO and PCV	cm-dm, mm-cm
$\delta\rho_R^{ARP_i}$	Receiver ARP (height)	cm-1 m
$\delta\rho_{Wind-Up_i}$	Phase Wind Up	cm-dm
N_i	Phase Ambiguity	-

(includes satellite and user position)

→ remaining are estimated as parameters

PPP models

Conventional

- Ionosphere-free linear combination
- 1st order ionospheric delay eliminated
- Well-established and convenient
- Only for two frequencies

IF

Uncombined

- Raw observations are processed
- Ionospheric delay is estimated
- Modern approach
- Any number of frequencies

UC

$$P_{IF} = \rho + c(dt_R^{GNSS_1} + \delta t_R^g) + dTrop^{wet} + \varepsilon$$

$$L_{IF} = \rho + c(dt_R^{GNSS_1} + \delta t_R^g) + dTrop^{wet} + \underbrace{\lambda_{IF} N_{IF}}_{\text{float}} + \varepsilon$$

Conventional model

Uncombined model

$$P_i = \rho + c(dt_R^{GNSS_1} + \delta t^g) - DCB_{1i} + dTrop^{wet} + \gamma_{1i} \cdot dIono_1 + \varepsilon$$

$$L_i = \rho + c(dt_R^{GNSS_1} + \delta t^g) - DCB_{1i} + dTrop^{wet} - \gamma_{1i} \cdot dIono_1 + \underbrace{\lambda_i N_i}_{\text{float}} + \varepsilon$$

+

ionospheric pseudo-observations

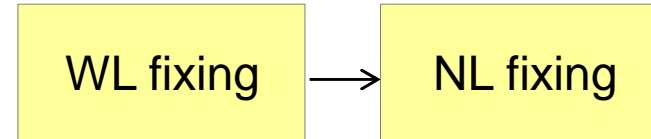
$$dIono_{pseudo} = dIono_1 + \varepsilon$$

→ uncombined model with ionospheric constraint

$$\text{float} = \text{integer} + \text{eliminate} - \text{correct}$$

$$\underline{N_{IF}} = \underline{\bar{N}_{IF}} + \underline{b_{R,IF}} - \underline{b_{IF}^S}$$

Conventional



float solution

epochs

Uncombined

$$\underline{N_i} = \underline{\bar{N}_i} + \underline{b_{R,i}} - \underline{b_i^S}$$

WL₁₂
WL₁₃ fixing
WL₂₃

+

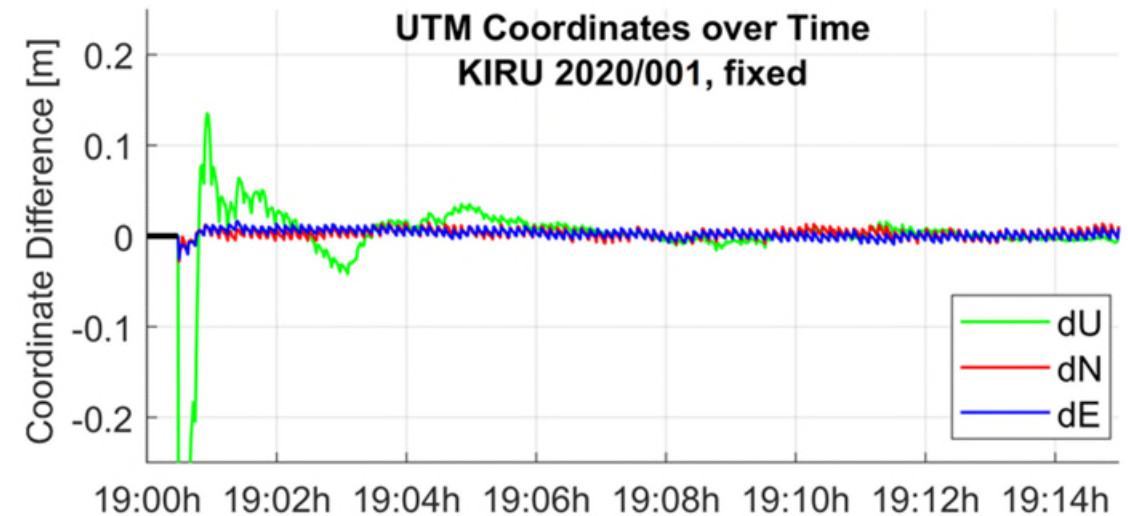
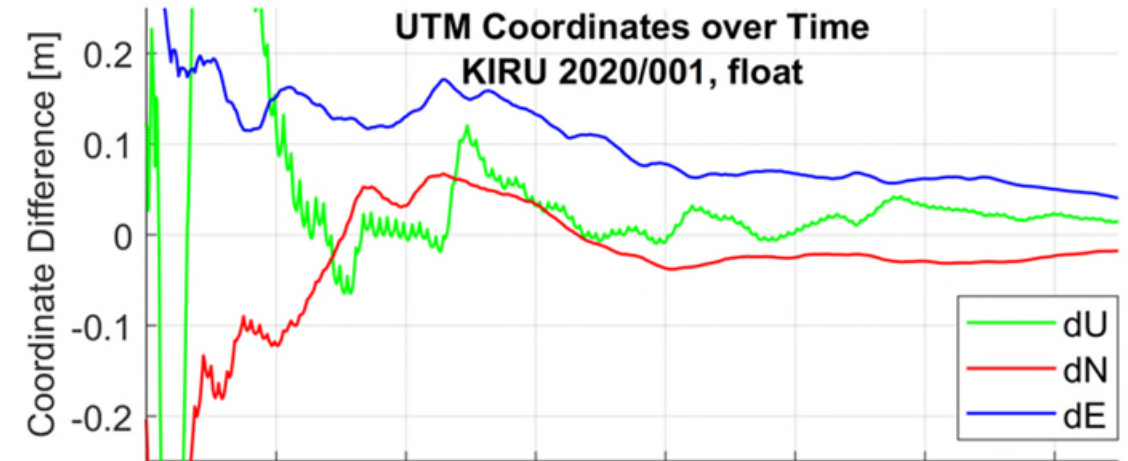
L₁ fixing

Float solution

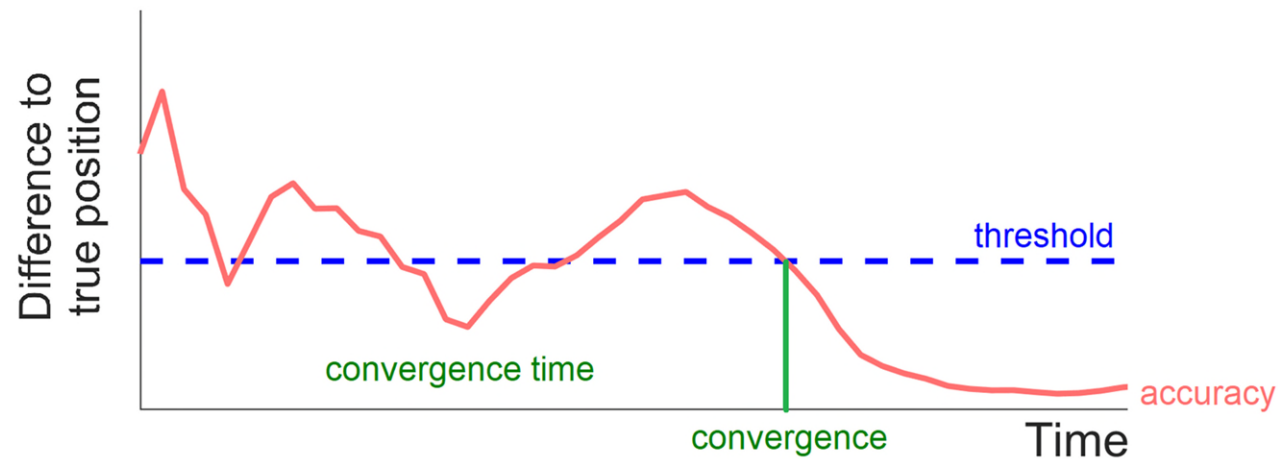
- Extended Kalman Filter

Fixed solution

- Fixed ambiguities are introduced as pseudo-observations
- Least-Square-Adjustment

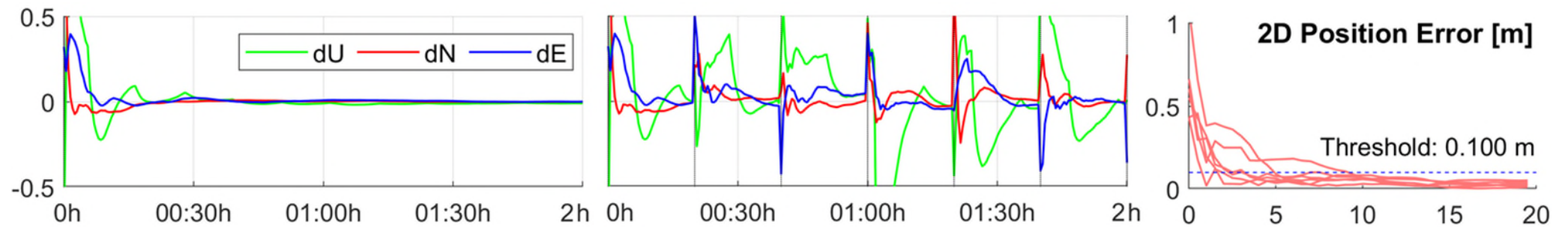


Convergence and accuracy



Coordinate convergence is achieved when the position difference reaches a specific level of accuracy and does not exceed this level after reaching it.

How to study the performance of PPP:



+ reference values (e.g., coordinates)

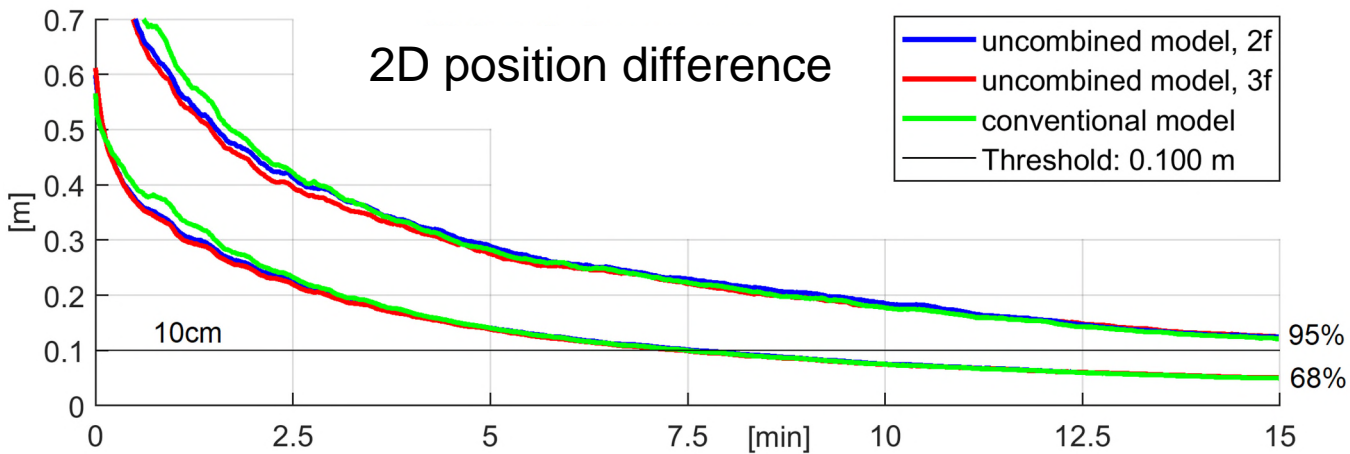
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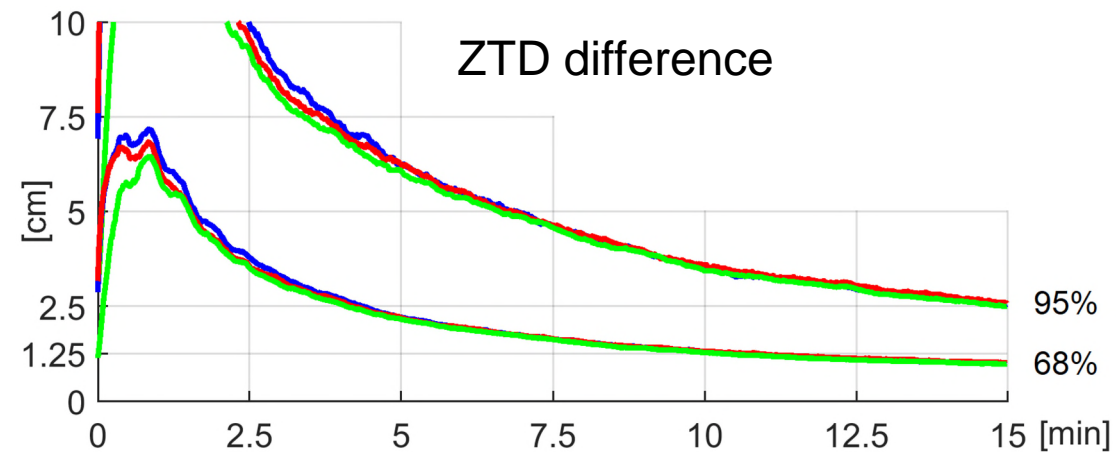
Float convergence

- Typical convergence time (2D < 10 cm): 7 min
- UC vs. IF:
 - First minutes
 - Difference vanishes
 - Accuracy similar

Coordinates

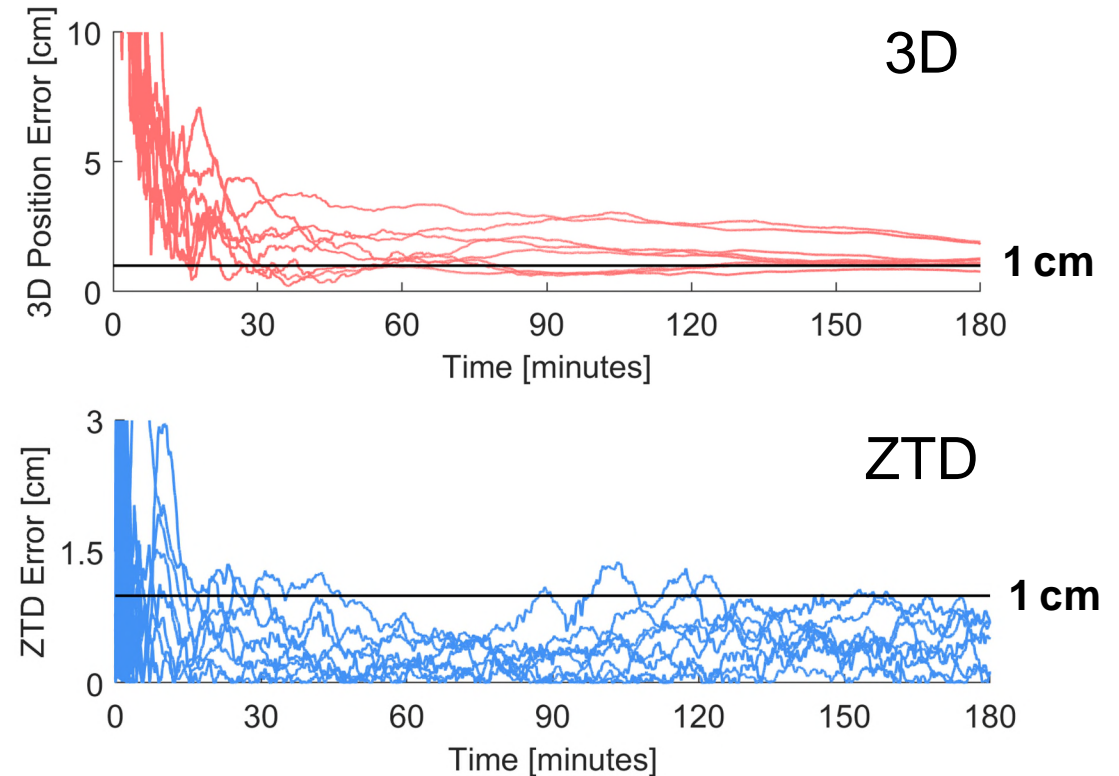


Tropospheric delay



Long-term performance

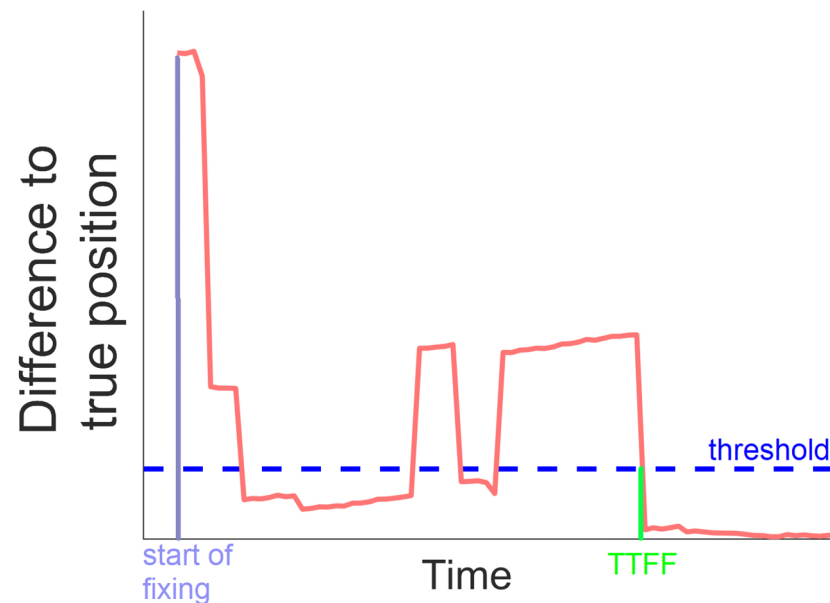
- Float coordinates and tropospheric delay
- At or below one-cm-level
- On the edge of the physical limits of GNSS



Arequipa, Peru

Aug 1, 2022

Time to first fix

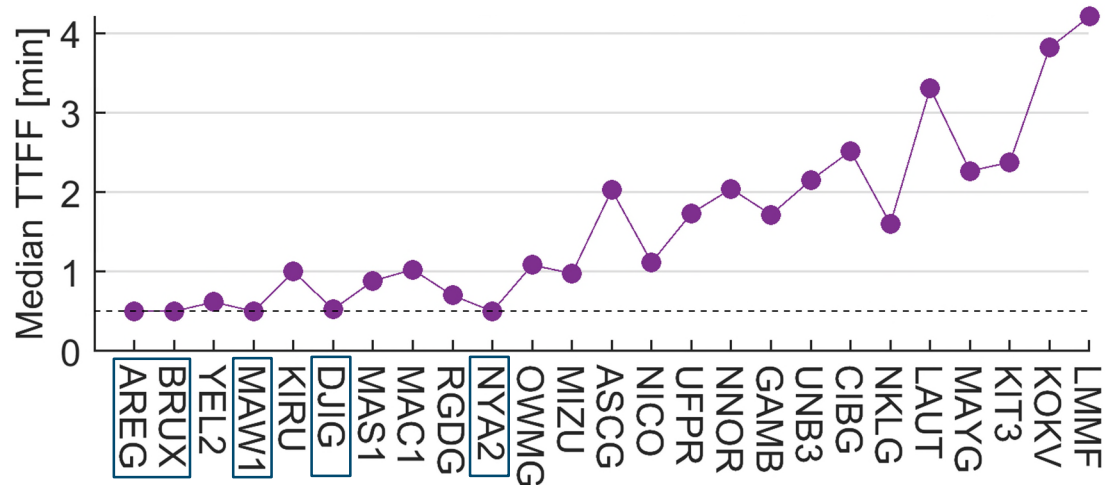


The time to first fix time (TTFF) is achieved when the fixed position reaches a specific level of accuracy and does not exceed this level afterwards ($2D < 5 \text{ cm}$).

Median TTFF

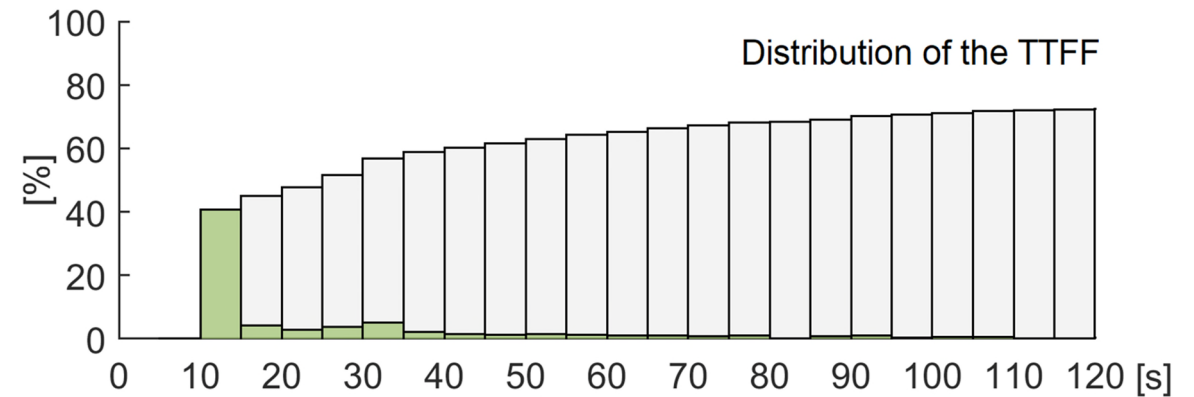
Global test case

- Fixing starts after 30 sec
- Stations perform differently
- Median TTFF: 30 sec to 4 min



Five best stations

- All operating a Septentrio PolaRx5 receiver
- Fixing starts after 10 sec
→ “instantaneous”

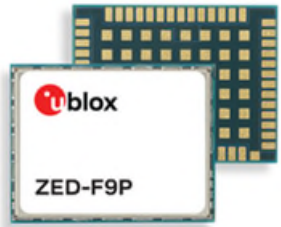


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Low-cost equipment

~200\$



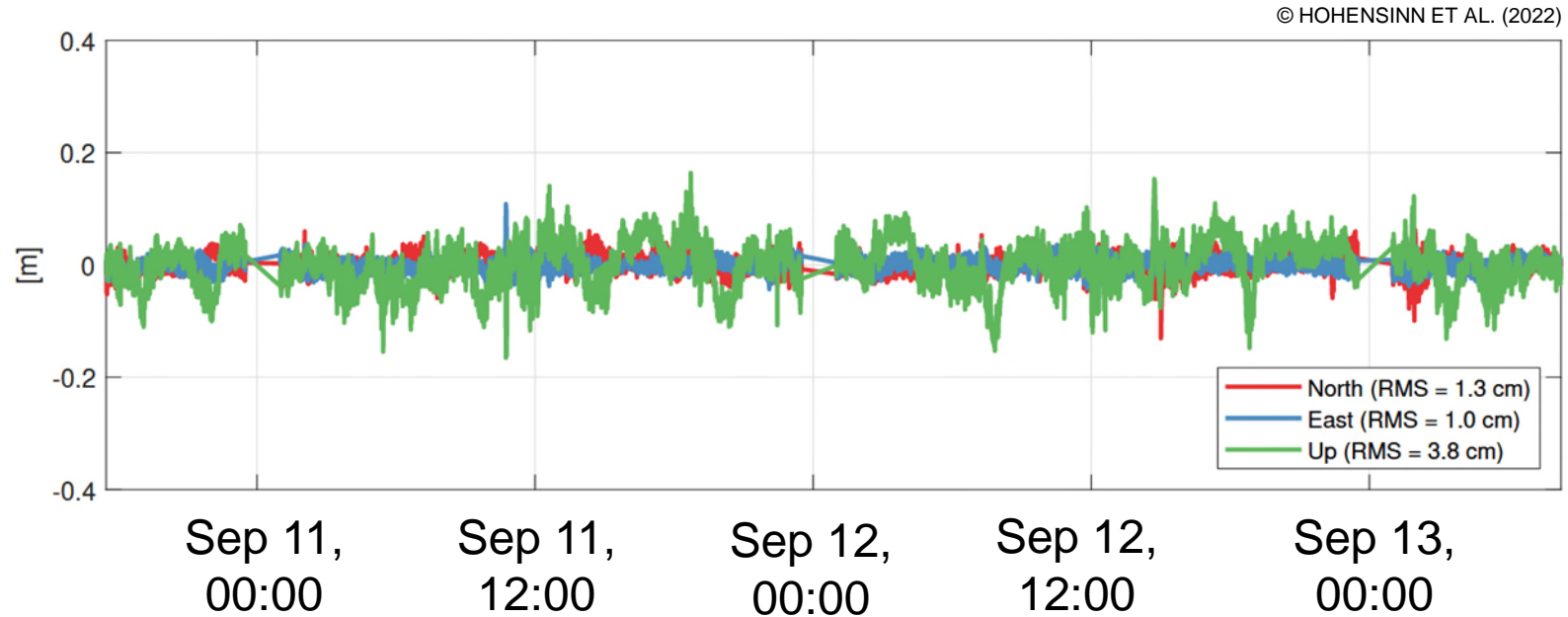
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+

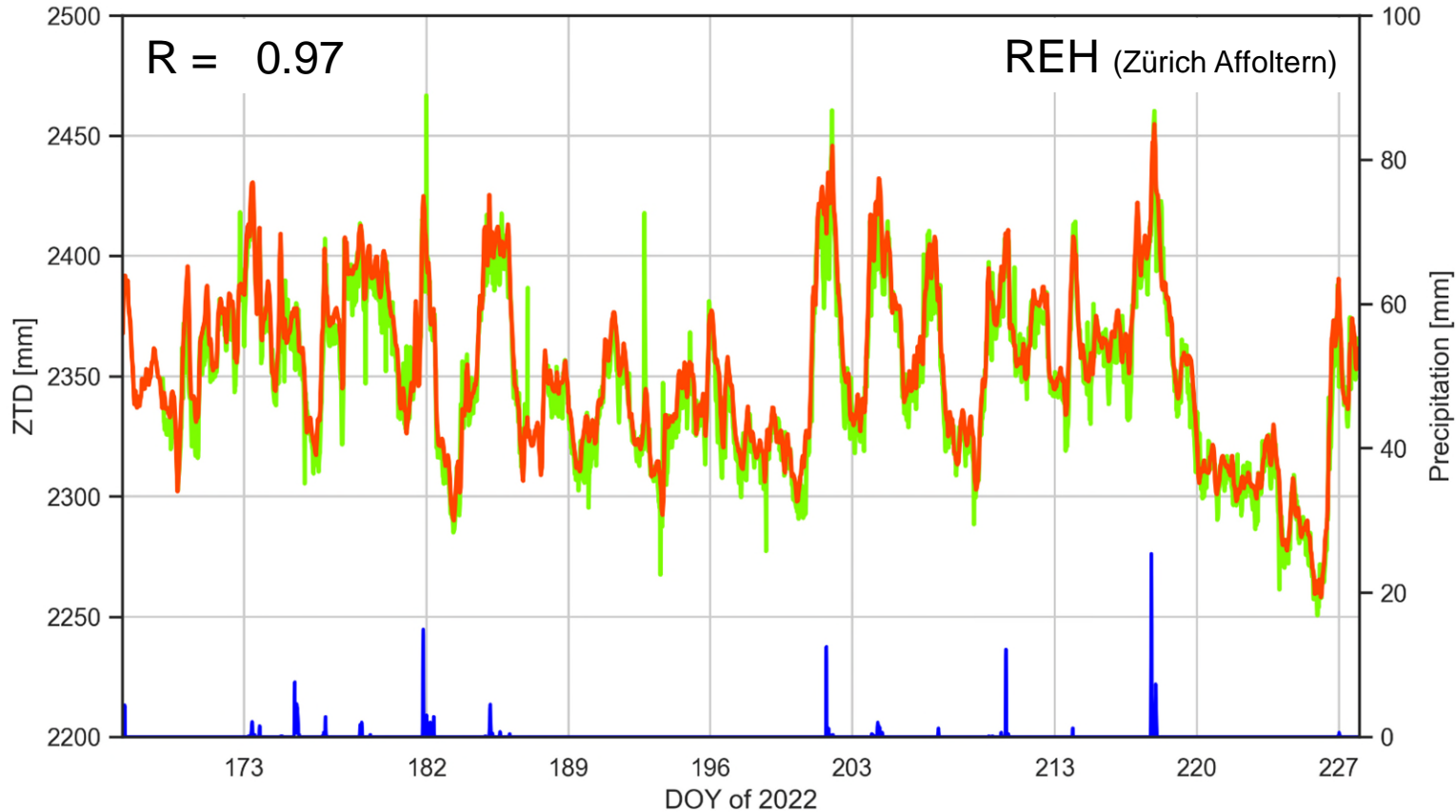
~100\$



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→ stable cm-level position with real-time settings



raPPPid vs. Bernese

rms = 10.61
 bias = 5.06 [mm]
 std = 9.33

raPPPid (real-time settings)
 Bernese (post-processing)
 Precipitation (measured)

© AICHINGER-ROSENBERGER ET AL. (SUBMITTED YESTERDAY)

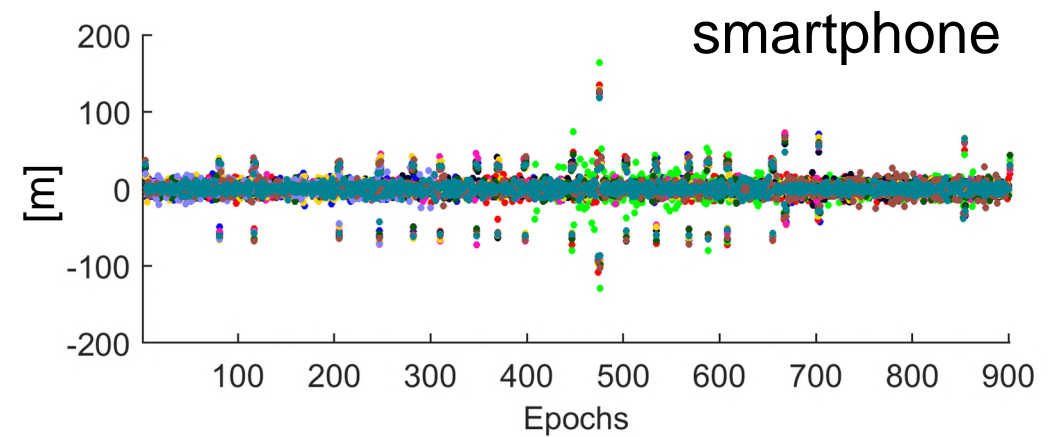
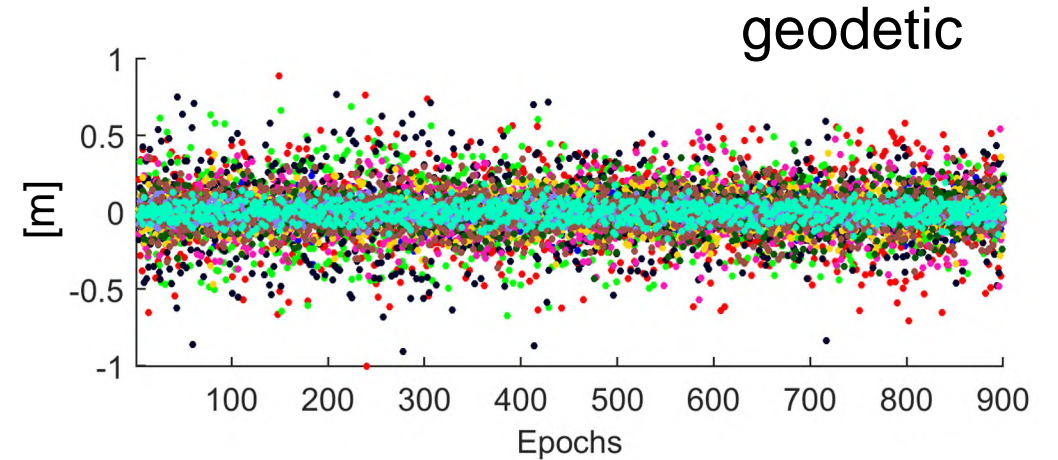
Smartphone + GNSS

- Since 2016, Android allows accessing raw GNSS measurements
- Enables self-developed GNSS algorithms
- Log GNSS measurements
- PPP processing with raPPPid



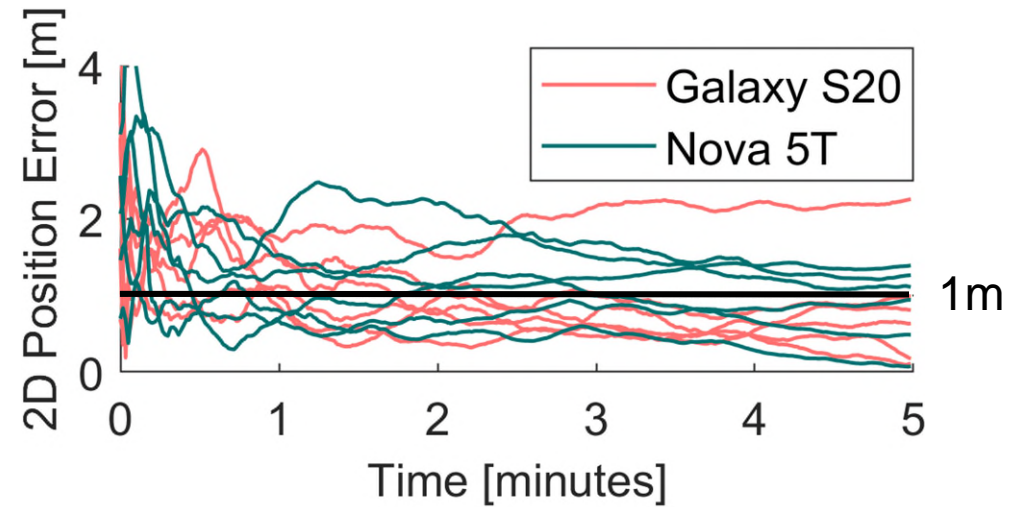
Observation quality

- Code observations
- 1 sec observation interval
- Build triple difference
- Just one of many examples...



Convergence

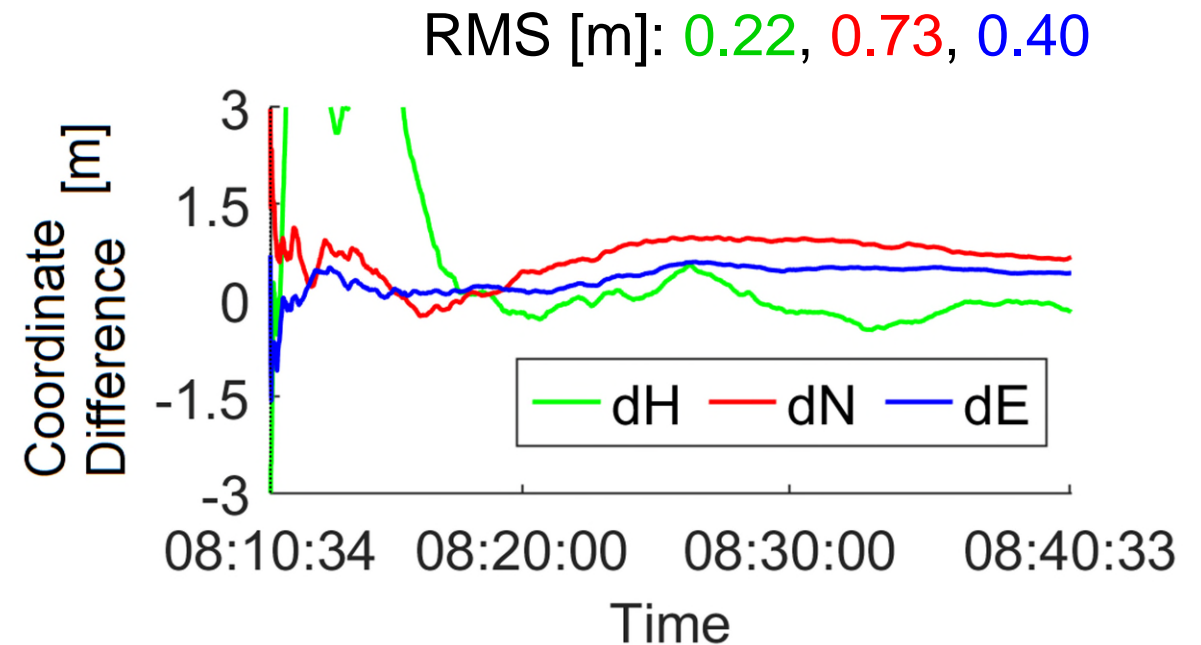
- Code only
- Few minutes
- 2D position error < 1 m



Samsung Galaxy S20 FE, Huawei Nova 5T

Long-term stability

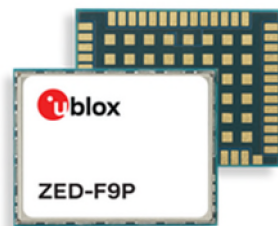
- Samsung Galaxy S20 FE
- 30 min period
- Stable decimeter-level accuracy



Performance

Low-cost

- Encouraging results
- Comparable to geodetic equipment



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Smartphone

- Various challenges
- Big potential (e.g., phase)
- < 1 m is possible



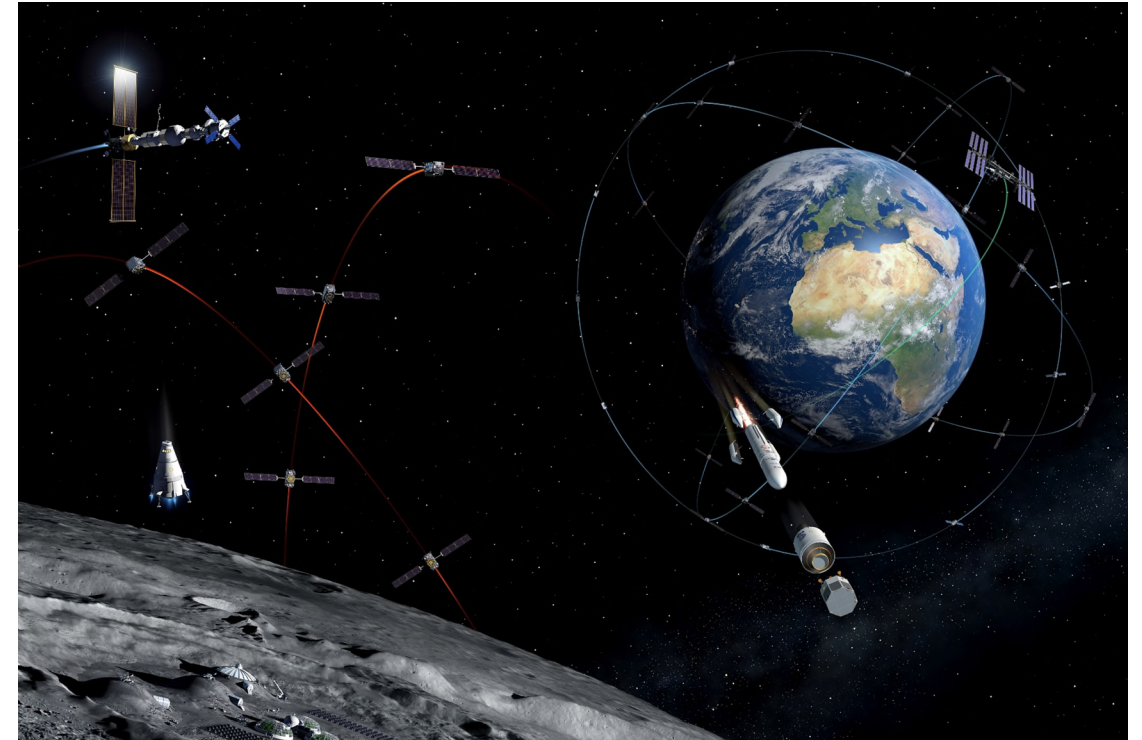
→ FFG-project: APPP

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Potential

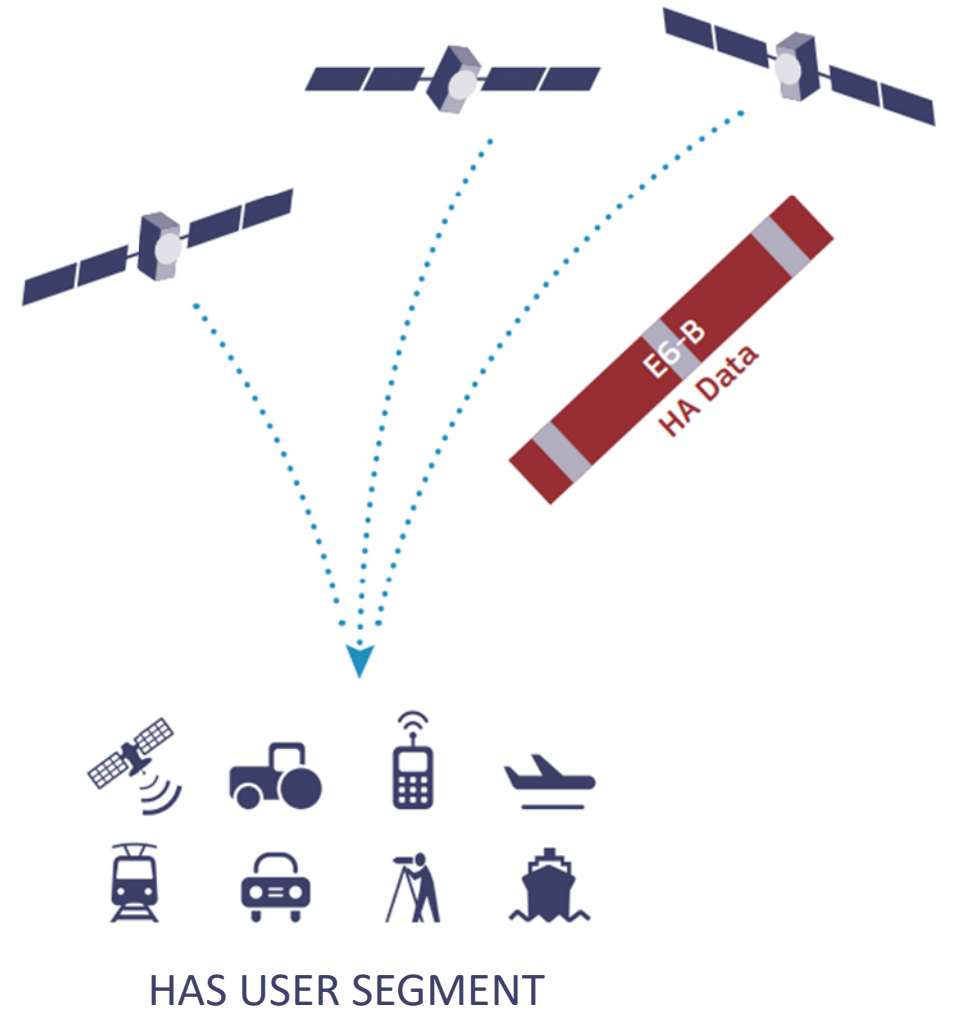
- Challenge well-established relative positioning methods like RTK
- Low-cost, low-quality, kinematic
- Combination and cooperation with other...
 - Techniques: reverse PPP,...
 - Sensors: accelerometer,...



Outlook

PPP is an upcoming positioning method:

- More available satellites and frequencies
- Advancing satellite products (e.g., Kepler)
- Instantaneous convergence?
- Galileo HAS



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**Thank you
for your attention!**

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