

Article

Improving Sentinel-1 Flood Maps Using a Topographic Index as Prior in Bayesian Inference

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Abstract: Sentinel-1-based flood mapping works well but with well-known issues over rugged terrain. Applying exclusion masks to improve the results is common practice in unsupervised and global applications. One such mask is the height above the nearest drainage (HAND), which uses terrain information to reduce flood lookalikes in SAR images. The TU Wien flood mapping algorithm is one operational workflow using this mask. Being a Bayesian method, this algorithm can integrate auxiliary information as prior probabilities to improve classifications. This study improves the TU Wien flood mapping algorithm by introducing a HAND prior function instead of using it as a mask. We estimate the optimal function parameters and observe the performance in flooded and non-flooded scenarios in six study sites. We compare the flood maps generated with HAND and (baseline) non-informed priors with reference CEMS rapid mapping flood extents. Our results show enhanced performance by decreasing false negatives at the cost of slightly increasing false positives. In utilizing a single parametrization, the improved algorithm shows potential for global implementation.

Keywords: synthetic aperture radar; Sentinel-1; flood mapping; Bayesian inference; hand above nearest drainage



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1. Introduction

In recent years, Earth-observation-based mapping and monitoring of floods has increasingly utilized synthetic aperture radar (SAR) data [1]. This situation can be attributed to the excellent systematic acquisition capabilities of the Copernicus Sentinel-1 mission [2]. In the past two years alone, multiple large-scale flood events have been monitored and analyzed in unprecedented detail using SAR-based methods [3,4]. These methods must work on time and provide accurate results, giving decision-makers actionable information for disaster relief, recovery, and reconstruction [5].

Previous studies have demonstrated SAR-based flood mapping workflows to work well, but with some well-known limitations [6–11]. Problems arise in areas where SAR data (only) flood retrievals become ambiguous. Examples are other low-backscatter areas, such as radar shadow regions, or no-sensitivity areas like dense vegetation. In some studies, localized parameterizations (e.g., changing thresholds) or more complex methods [12–16] address these concerns but are seldom near-real-time (NRT) or globally viable.

Other workflows rely on exclusion masking of these problematic areas [8,17]. While masking is a reasonable solution, over-application is a concern and should be minimized. One commonly used masking method that minimizes misclassification of SAR flood lookalikes uses the height above the nearest drainage (HAND) index [18,19]. HAND masking, while known to work well in removing false positives based on topography [8,20], often affects significant portions of a flood scene, rendering the mapping algorithm futile for these parts. Despite this concern, HAND masking's simple execution and robust global performance make it an ideal inclusion in operational workflows [21].

One flood mapping algorithm in operational use for the new Global Flood Monitoring service [22] of the Copernicus Emergency Management Service (CEMS, <https://emergency.copernicus.eu/>, accessed on 14 September 2023) is the TU Wien flood mapping algorithm. This method is based on a probabilistic Bayesian method [23] that can integrate pre-existing information (from auxiliary sources) to arrive at improved decisions or classifications. However, using other information to form prior probabilities (or *priors* for short) is often overlooked in SAR-based flood mapping efforts in favor of non-informed priors [24]. In doing so, they miss the potential to improve areas where SAR backscatter alone is ambiguous or problematic. With limited studies having shown success [5,25] and others presenting evidence to the contrary [24], a systematic study of priors in Bayesian SAR-based flood mapping is needed.

This study aims to improve the TU Wien flood mapping algorithm. To accomplish this, instead of using it for masking, we leverage the HAND index to derive priors. We introduce a HAND prior probability function, derive globally applicable parameters, and show its performance on flooded and non-flooded cases in six study sites across the globe.

2. Height above the Nearest Drainage as a Prior

2.1. SAR Flood Mapping Using Bayes Inference

Bayesian classifiers are probabilistic classifiers that apply Bayes' Theorem. In Earth observation applications, particularly flood mapping applications, these classifiers are usually applied at the pixel level. Pixels are classified as flooded when the probability after inference, or the so-called posterior probability, exceeds a pre-defined threshold (usually 50%). One can calculate the posterior probabilities from Bayes' inference using:

$$p(F|\sigma^0) = \frac{p(\sigma^0|F)p(F)}{p(\sigma^0|F)p(F) + p(\sigma^0|N)p(N)} \quad (1)$$

where $p(\sigma^0|N)$ is the conditional probability for a pixel being non-flooded and $p(\sigma^0|F)$ for the flooded case, while $p(F)$ and $p(N)$ are the prior probabilities of a pixel being flooded and non-flooded respectively. Most literature has focused on formulating the conditional probability functions, using:

- *Observed SAR parameters*: backscatter intensity [23,24], backscatter difference [26], or coherence [25];
- *Probability distribution models*: Gaussian [23,25–27] against non-Gaussian [24];
- *Dataset used as a reference for flooded probability distribution*: scene-based [24,25,27] or historically sampled [23,26];
- *Dataset used as a reference for non-flooded probability distribution*: scene-based [24,25,27] against time-series-derived [23,26].

In the case of the TU Wien algorithm [23] tested in this study, $p(\sigma^0|N)$ is derived from a harmonic model describing the local VV backscatter, expressed as the expected sigma-naught value (σ^0 or SIG0) for a given day of the year. $p(\sigma^0|F)$ is estimated from calm water samples, taken at different locations over sea and lakes at times without strong winds.

On the other hand, prior probabilities are often reduced to the non-informative case [26,28], i.e., equal chances of being flooded or non-flooded. Giustarini et al. justified this assertion by testing varying prior probability values without significantly affecting the reliability metric of their flood maps [24]. Further testing priors based on flooded area percentages from reference datasets also did not significantly improve the results in their study. However, their study applied prior values uniformly across their study areas and did not investigate priors that spatially vary.

Reffice et al. discuss the possibilities of such localized priors in their study [25]. Their study demonstrates a prior probability distribution function from the inverse distance to rivers. Moreover, their subsequent work with a Bayesian network included a piecewise geomorphic-flooding-index-based function as an auxiliary input [5]. While both

functions offer simple solutions, their approach involves localized optimization of their proposed functions.

2.2. HAND-Based Prior Probability Function

HAND is a hydrological model derived from terrain data such as digital elevation models (DEMs) [19]. As an index, it is often utilized in SAR-based flood methods to exclude improbable flooded pixels [29], specifically for low-backscatter pixels above a pre-defined height threshold relative to the nearest drainage level. In machine learning-based flood mapping algorithms, it has also been used as an auxiliary input [30]. Notably, flood modelers use HAND with synthetic rating curves for rapid inundation mapping [31–33], and it has been touted for its performance despite its simplicity.

Our hypothesis is that the HAND index is an ideal candidate prior information in the global operational context because: (1) as there are several (near-) global DEMs openly available, it can be computed globally [34,35], (2) it is a simple model (applied the same way everywhere), and (3) it does not require regular updates (since most terrains are primarily stable).

Considering this, we conceptualize a prior probability function that shares HAND's robustness and simplicity. Thus, only the HAND index is used as an input in our Bayesian inference formulation to estimate the flooded prior probabilities, $p(F)$, while the non-flooded prior, $p(N)$, is computed from $1 - p(F)$. For $p(F)$, we propose an exponential function $p(F|h)$ given as follows:

$$p(F|h) = \frac{1}{1 + e^{\frac{(h-\mu)}{\sigma}}} \quad (2)$$

where

h = HAND index value per pixel

μ = midpoint

σ = steepness

The midpoint (μ) defines the HAND value where the probability indicates a 50% chance of the pixel being labeled as water. In contrast, the steepness parameter (σ) dictates the degree to which the resulting probability changes per increase in HAND value, essentially controlling the function's characteristic shape. A lower σ value (e.g., $\sigma < 1$) results in a function behaving like a step(down) function, while a higher σ value (e.g., $\sigma > 30$) leads to an almost linearly decreasing function.

Figure 1 illustrates the response of the proposed function to varying steepness parameter, here centered at $\mu = 20$. This exponential formulation models a gentle decrease in probabilities at lower HAND values where flooding is more likely to occur, while having a steeper decline towards the midpoint where floods are less likely to happen.

Similar exponential functions have been proposed by Refice et al. for their distance-to-river function [25] and Jafarzadegan et al. for their log-normal flood probability function used for HAND-based flood mapping [31]. The latter reports a similar function being stable during parameter optimization, showing robustness to parameterization, a preferred characteristic for global operations [36].

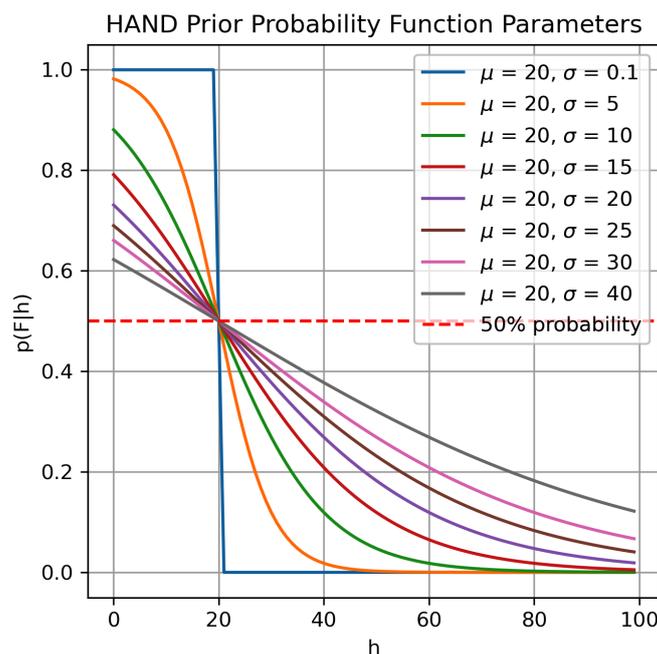


Figure 1. HAND prior probability function response to varying steepness (σ) at midpoint (μ) = 20. Y-axis indicates the probability $p(F|h)$. X-axis indicates the HAND values (h).

3. Materials and Methods

3.1. Study Sites

To test the performance of Bayesian flood mapping with HAND priors, we analyzed flood events and no-flood cases at six test sites covering different geographical regions, climatic conditions, and terrain properties. The details are described in Section 4.2. Table 1 shows an overview of these six test sites.

Table 1. Test Sites and Matching CEMS Activations with Flood Event Dates and No-Flood Dates.

CEMS Activation	Type	Location	Flood Event Date	No-Flood Date
EMSR569	Flood	Valencia, Spain	22/03/2022	21/03/2021
EMSR577	Flood	Suriname	16/06/2022	09/06/2021
EMSR586	Flood	New South Wales, Australia	05/07/2022	16/06/2021
EMSR637	Flood	New South Wales, Australia	24/10/2022	17/10/2021
EMSR639	Flood	Belize	03/11/2022	27/10/2021
EMSR640	Flood	Scotland, United Kingdom	20/11/2022	25/11/2021

The flood events were identified from available Copernicus Emergency Management Service (CEMS) [37] rapid mapping activation covering flood events mapped with Sentinel-1 as satellite data input from March to November 2022. This ensured having reference flood extents for our analysis that match our generated flood maps exactly spatially (minimal resolution and sampling effects) and temporally (no time lags).

3.2. Materials

3.2.1. Sentinel-1 Databcube

The Sentinel-1 databcube curated and managed by TU Wien and EODC [38] serves as the primary data source for the Bayesian flood mapping workflow [23] employed in this study. This databcube was generated from Sentinel-1 Ground Range Detected (GRD) datasets [39], which are sampled at a 20 m \times 20 m pixel size and tiled at the T3 tiling level (300 km extents) of the Equi7Grid system [40]. The matching SAR images with the VV polarization band for the six flood events were queried from this databcube. Harmonic

parameters were also derived from this datacube [41] to estimate the day-of-year no-flood reference for the pixel-based flood inference.

3.2.2. Height above the Nearest Drainage

Deriving the HAND index is a reasonably straightforward raster-based methodology using hydrologically conditioned digital elevation models [19]. While several global HAND datasets are openly available [35,42], we computed HAND index datasets from 90 m SRTM [34] using a Python script with ArcGIS (10.x) ‘Spatial Analyst Tools.tbx’ and ‘Topography Tools 10_2_1.tbx’. This dataset was resampled at a 20 m resolution and tiled to align with the Sentinel-1 datacube.

Locally improving HAND by optimizing the contributing drainage area is recommended [35]. However, good performance as an exclusion mask with global parameters [21] has been shown to work for SAR-based flood mapping without such optimization. Thus, no localized optimizations were undertaken.

3.2.3. Reference Flood Extents

Obtaining ground truth data for flood mapping is not always possible [43]. A reasonable alternative is using existing, manually quality-controlled flood extent maps, such as those made available through CEMS. Using the criteria described in Section 3.1, CEMS reference vector flood extents and associated ancillary data (e.g., AOI, Hydrology) [44] were downloaded from <https://emergency.copernicus.eu/> (accessed 14 September 2023). The downloaded reference datasets were subsequently rasterized, reprojected to the Equi7grid tiles, and masked to match the area of interest (AOI) in preparation for the assessments. To better match the flood maps generated with the CEMS flood reference, we used the same CEMS hydrology dataset (rivers, lakes) as a water mask to differentiate flooding from permanently inundated areas [45].

3.3. HAND Prior Probability Function Parameter Estimation

First, we determined the globally appropriate midpoint (μ) and steepness (σ) parameters for the HAND prior probability function through the iteration and analysis of the average critical success index (CSI), user’s accuracy (UA), and producer’s accuracy (PA) of all test sites relative to their CEMS counterparts.

CSI, defined by Equation (3), was used because it is a robust estimator of overall flood map performance [46]. Furthermore, UA and PA, defined by Equations (4) and (5), were also used to discern over- and under-estimation tendencies of the proposed improvement. While no assessment metric is without issues, these metrics were selected to reduce dependence on the size of flood extents [47]. These metrics are computed from the binary confusion matrix of a classified map versus a reference. All assessment metrics are defined by four binary confusion matrix elements, namely: true positive (TP), true negative (TN), false positive (FP), and false negative (FN).

$$CSI = \frac{TP}{(TP + FP + FN)} \quad (3)$$

$$UA = \frac{TP}{(TP + FP)} \quad (4)$$

$$PA = \frac{TP}{(TP + FN)} \quad (5)$$

Given the definition of the midpoint (μ), we selected our iteration range based on the published values used as HAND exclusion mask thresholds with typical optimization ranges from 5 to 40 m and selected value ranges from 10 to 20 m [15,31,48]. Value ranges in the same magnitude were tested for the steepness (σ) to maintain a reasonable steepness of the resulting function.

For each combination of these two parameters, spatially varying HAND-based prior probabilities were computed for flood map generation. Then, the accuracy metrics (against the CEMS reference) were computed, tabulated, and averaged per parameter combination for all test sites. Finally, the estimated optimal parameters were selected based on the maximization of the three metrics.

3.4. Comparative Performance

Using the determined HAND function, we compared the flood maps generated with non-informed priors and HAND-derived prior probabilities to show their performance in flooded and non-flooded scenarios. Figure 2 shows the TU Wien flood mapping flowcharts of the two cases, highlighting the difference between the two workflows, consisting of (1) type of input priors and (2) (non-)removal of the HAND mask post-processing step.

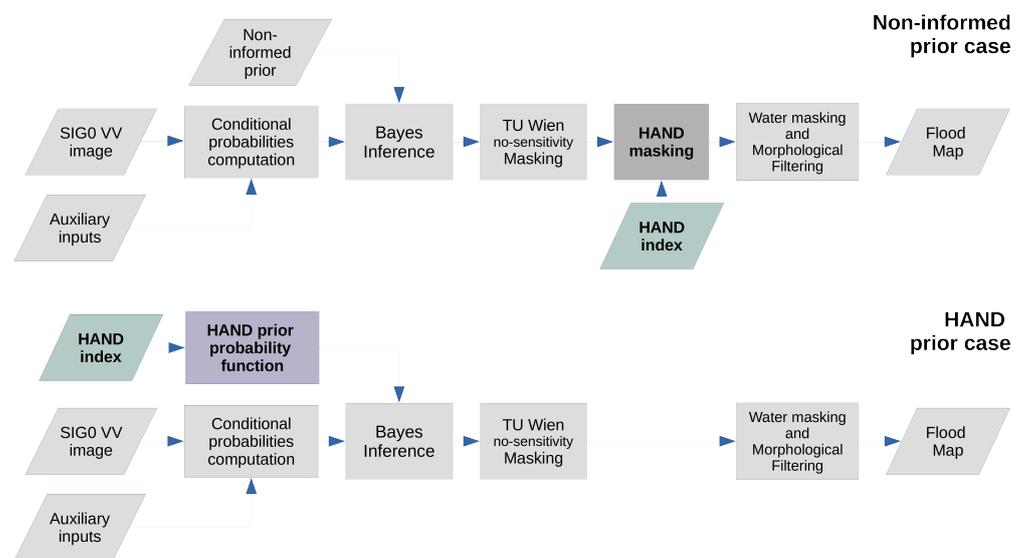


Figure 2. Simplified TU Wien flood mapping flowcharts. Non-informed prior probability case (above). HAND prior probability case (below). Details of the other auxiliary inputs and the TU Wien no-sensitivity and probability distribution-based masking workflow are detailed in the work of Bauer-Maschallinger et al. [23].

As earlier described, raster-based prior probabilities were generated from the HAND dataset using Equation (2). These prior probabilities were used for the first set of test cases, which we refer to as the HAND prior cases. In contrast, a spatially uniform 0.5 prior probability was used for the second set of test cases for the non-informed prior cases. HAND exclusion masks (using the matching μ) were applied as a post-processing step for non-informed prior cases, while this was skipped for the maps computed with HAND prior cases.

Flood maps with both prior cases were generated for flooded-scene scenarios, covering the six flood events. We then computed the (above-mentioned) assessment metrics against the matching pre-processed reference CEMS flood data. After this, we examined the differences in the three metrics between the prior probability cases. Exemplary confusion maps of each site were also created to qualify these differences.

In many cases, flood mapping algorithms are tailor-fitted to work for flooded scenes, which may have a negative effect for monitoring non-flooded scenarios. If an algorithm is applied to a non-flooded image, false positives should not be excessive to give the impression of a scene being flooded. This is important for global monitoring applications where not all results can be manually vetted.

However, in non-flooded scenarios, we lack true positives; thus, the CSI, UA, and PA metrics are not applicable. In their place, we calculated the false positive rate (FPR) [49]

defined by Equation (6) for maps using both prior cases on exemplary non-flooded images for the same study sites. Here, the binary confusion matrix was generated with a synthetic all-no-flood pixels as reference. In effect, all identified floods are false positives, while non-flooded pixels are true negatives.

$$FPR = \frac{FP}{FP + TN} \quad (6)$$

The exemplary images were selected to match the same vegetation state as the flooded images. Thus, images approximately one year earlier were identified and matched by orbit to ensure almost identical imaging geometry. These image acquisition dates are noted in Table 1. While not explicitly screened, no extraneous SAR effects (abnormally high or low backscatter for a scene caused by extremely wet, dry, or windy conditions) were observed in the selected images.

4. Results and Discussions

4.1. Prior Probability Parameterization

We averaged the CSI, UA, and PA of all six sites across all the parameter iterations to discern an optimal estimate of the function parameters μ and σ . As noted earlier, the function response does not significantly change for small parameter changes; hence, for our purpose, the iteration by 5 m of both parameters up to 40 m—leading to 64 combinations—is adequate to arrive at a reasonable estimate of the HAND prior probability function. We plot the metrics for all the combinations for the HAND-based prior function and the non-informed prior case as a reference.

As seen in Figure 3, panel (a), the best average CSI values were observed with μ between 20 and 35 m and σ between 5 and 10 m. Moreover, the highest CSI was observed with $\mu = 30$ m and $\sigma = 10$ m. It should be noted that the CEMS rapid mapping activation uses both the VV and VH bands [3], while this study focuses on the existing TU Wien workflow using VV polarization only, which could explain the low average CSI values. (We scrutinize these further on a study site basis in Section 4.2). In terms of thresholding, VH polarization has a slight advantage in mapping complex floods or transition areas, as it more likely exhibits a decrease in backscatter intensity compared to VV polarization, which is more sensitive to complex scattering mechanisms [50].

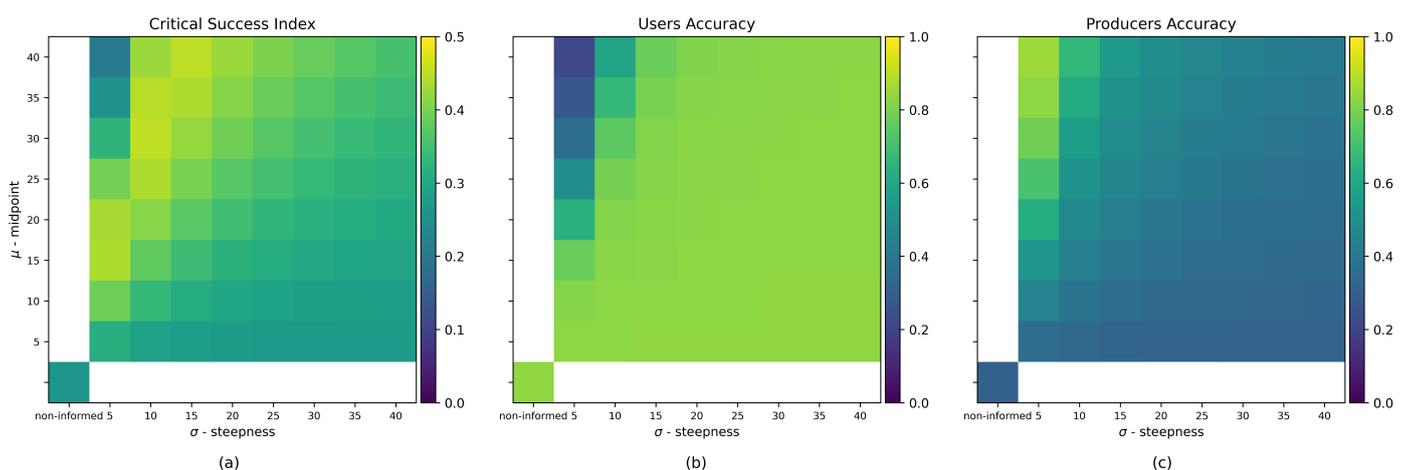


Figure 3. The average comparative metrics of the study sites versus the prior probability function parameterizations. (a) Average critical success index, (b) average user’s accuracy, and (c) average producer’s accuracy. Y-axis indicates the midpoint (μ). X-axis indicates the steepness (σ). The lower left panel shows the non-informed prior case for reference.

As our objective for this study is to improve the algorithm, the absolute CSI values are less important than the observed difference compared with the baseline non-informed prior

case. For reference, the overall accuracy values in all test cases for all sites exceeded 87%. They are not presented here for brevity, as the CSI is sufficient to highlight the differences in the overall performance.

On the other hand, the HAND prior parameter combinations and reference non-informed prior results have in general high UA values but show significantly lower values at low σ values. The PA values, similar to CSI, are not ideal. Most combinations do not significantly change the UA (b). Furthermore, a significant decrease in the UA is observed at σ between 5 and 10, with a reasonable decrease at μ less than 25. Lastly, the PA plot in panel (c) shows an increasing value with μ but a decreasing value with σ .

Since no combination shows a clear maximum for all three metrics, we can limit the parameter selection to $\mu = 25$ and $\sigma = 10$ or $\mu = 20$ and $\sigma = 10$ to minimize the decrease in UA while retaining a good CSI and PA improvement. We chose the latter as a conservative estimate for the function parameters.

4.2. Comparative Results HAND Prior

In the following, we describe in detail the performance of this selected parameterization. From Figure 4, it can be observed that the overall performance on all test sites, except the Suriname test site, has a significantly improved CSI and PA at the expense of a slight decrease in UA.

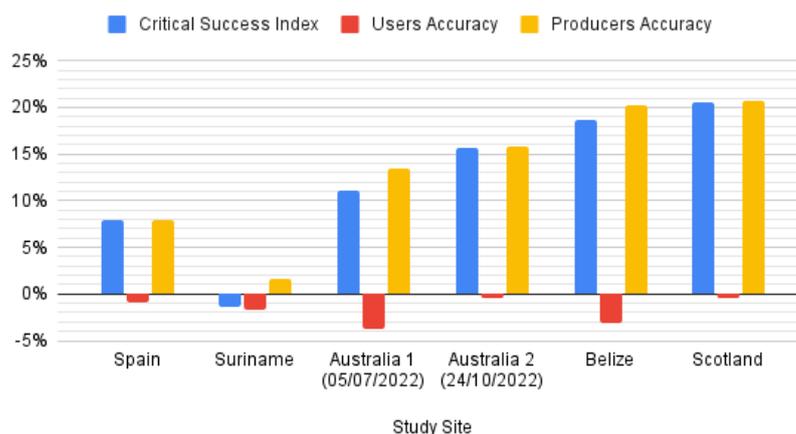


Figure 4. Differences between the comparative metrics. HAND prior case minus non-informed prior case.

Interestingly, the study sites that showed the significant improvement in CSI are areas with rolling terrain (Scotland) and low-lying wetland areas (New South Wales, Australia). The improvements are small for urban terrain (Valencia, Spain) and relatively flat areas. This result may be related to the limitation of HAND as a model for relatively flat areas [32], which in turn is often traced to discrepancies in the source DEM in these areas [51].

The following sections show confusion maps with water masks overlaid for reference [45]. We look at the details of the confusion maps of both HAND prior cases and non-informed prior cases to better understand the summarized findings.

4.2.1. Spain

The flood extent from Valencia, Spain, seen in Figure 5 primarily affected the river Turia and the adjacent green areas. The flooded area visible in the SAR flood maps is centered on its artificial channel. The channel is dotted with varying densities of vegetation. Dense foliage act as a volume scatterer and blocks the impinging signal from reaching the water surface. Thus, sections of the flood along the channel are not visible in the SAR flood maps.

False negatives along the edges of the channel (red arrows) are the most pronounced issue for the flood maps generated, which result in a very low CSI and UA. The channel is characterized by a relatively steep embankment, acting as a transition area and resulting in a complex scattering mechanism where the decrease in backscatter is not as pronounced.

The wider flood extent is better identified by the HAND prior case (b) than the non-informed prior case (a), causing the improvement in PA and CSI. For the most part, the HAND data reflects the low elevations of the channel. However, the resolution of the HAND data (e) is too coarse to cope with the misclassified pixels at the edges. The reference data and flood maps also miss the dense vegetation in the channel (yellow arrows); in this case, even with the highest possible prior probability of being flooded, it is not enough to overturn the non-flood result.

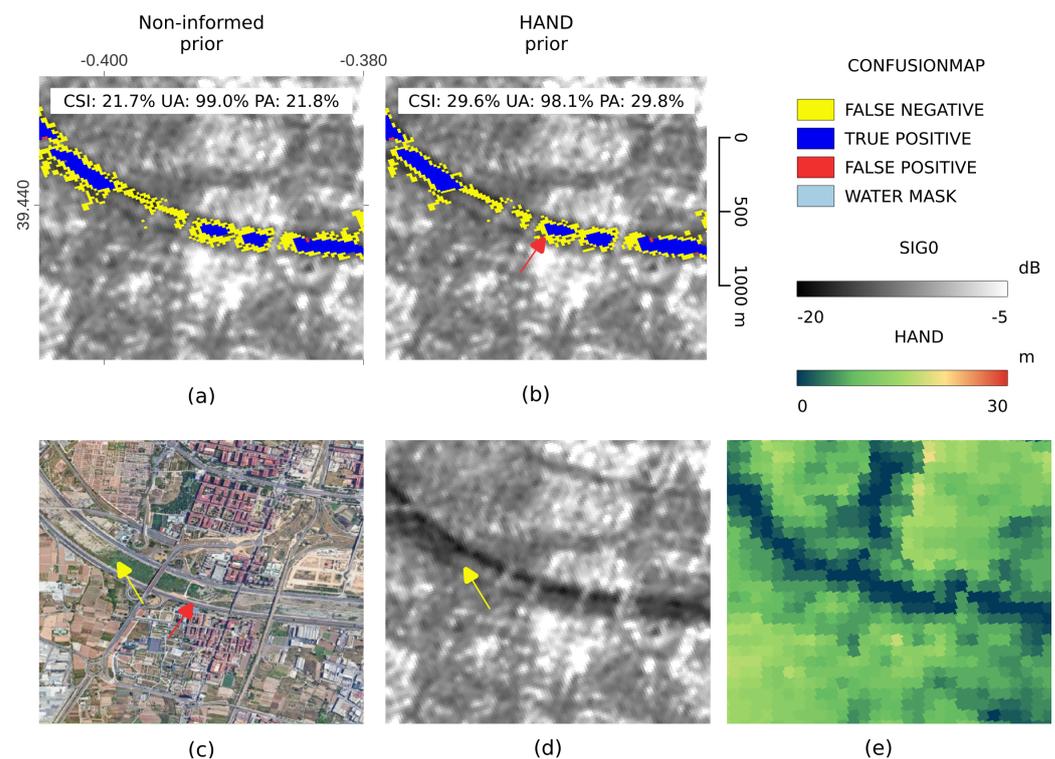


Figure 5. Confusion map of a portion of the Spain study site. Top row: confusion maps for non-informed prior case (a) and HAND prior case (b). Bottom row: true color Google satellite map (c), SIG0 backscatter intensity at VV polarization (d), and HAND index map (e)

4.2.2. Suriname and Belize

The result for the Suriname test site is shown in the top row of Figure 6; the area is near Grand Santi, French Guiana. The flood scene indicates overflow along the Marowijne River at the border of Suriname and French Guiana at several small locations. For this site, the HAND prior case does not seem to add value to the original method.

Only minor changes between the HAND prior case (a) and the non-informed prior case (b) were observed at this study site. Since the area is densely vegetated, the quality of the SRTM DEM to represent ground topography is in question [52,53]. As observed, most areas have relatively similar and relatively higher HAND values (c) outside the drainage network compared to the other sites, possibly confirming the tree canopy height issue. Thus, the method shows issues due to limitations of the input DEM affecting the HAND prior case performance.

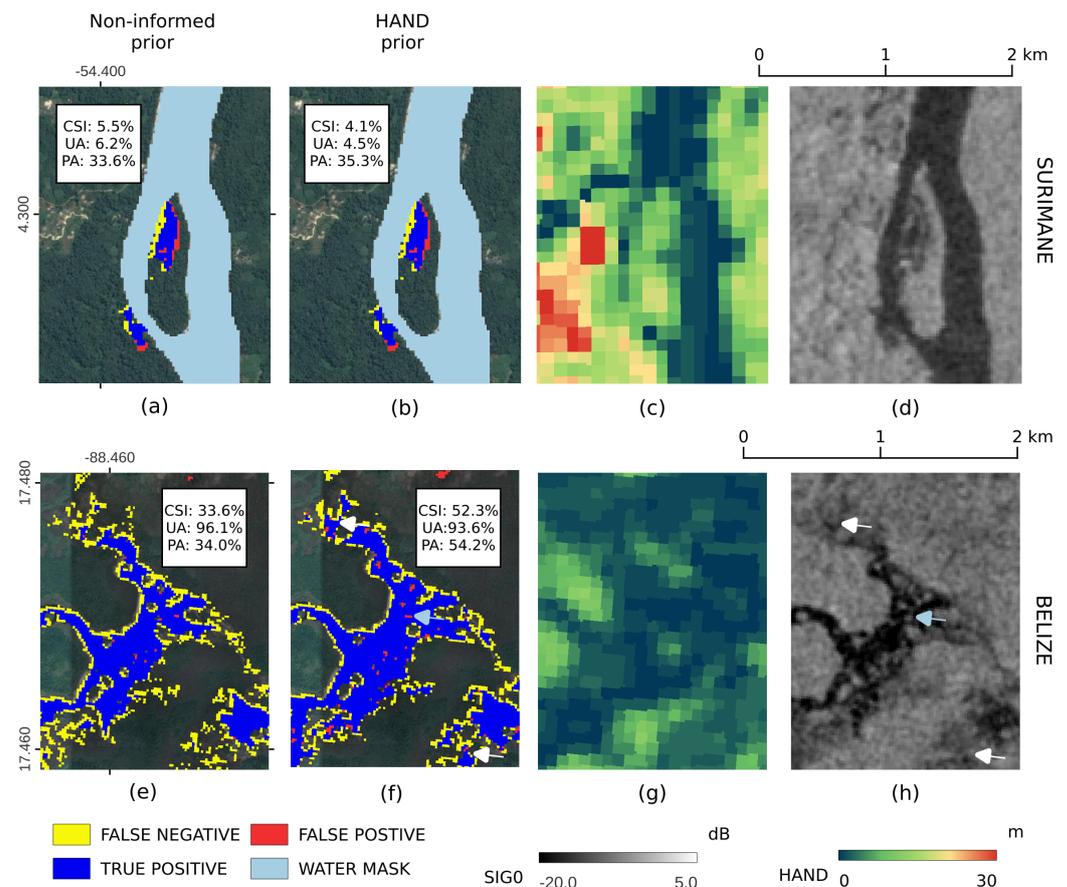


Figure 6. Confusion map of a portion of the Suriname and Belize study sites. Top row: Confusion maps for the Suriname study site overlaid on Google satellite map for non-informed prior case (a) and HAND prior case (b); HAND index map (c) and SIG0 backscatter intensity at VV polarization (d). Bottom row: Confusion maps for the Belize study site overlaid on Google satellite map for non-informed case (e) and HAND prior prior case (f); HAND index map (g) and SIG0 backscatter intensity at VV polarization (h).

The bottom row of Figure 6 features the Belize study area, focusing on an area west of Hattieville, Belize. Similar to the Suriname site, most of the area is covered by dense vegetation, but with noticeable patches of sparsely vegetated areas. The confusion maps (e and f) show floods for low-lying clearings. Here, possible flooded vegetation with less considerable decrease in backscatter intensity and flood edges are the most common sources of false negatives in both prior case flood maps. Some of these areas are corrected in the HAND prior case (white arrows). False positives are observed in the HAND prior case not present in the non-informed prior (blue arrow) are pixels with higher backscatter values compared with the surrounding flooded pixels.

4.2.3. Australia

Located in different parts of New South Wales, the 05/07/2022 (Australia 1) and 24/10/2022 (Australia 2) flood events share similar terrain characteristics. Both are located in low-lying areas littered with swamps, creeks, and streams. The 05/07/2022 (Australia 1) event covered the swampy area north of the Hunter River, while the 24/10/2022 (Australia 2) event occurred further inland near the town of Gunnedah and the Namoi River.

Both events cover substantial areas, as seen in Figure 7. False negatives along the flood borders (or transition zones) are a common issue for both the HAND prior cases (b) and (f) as well as the non-informed prior cases (a) and (e). The HAND prior case showed superior

performance in both flood events. Also worth noting are false positives (white arrows) that suggest this area is within the swampy region that is most likely flooded.

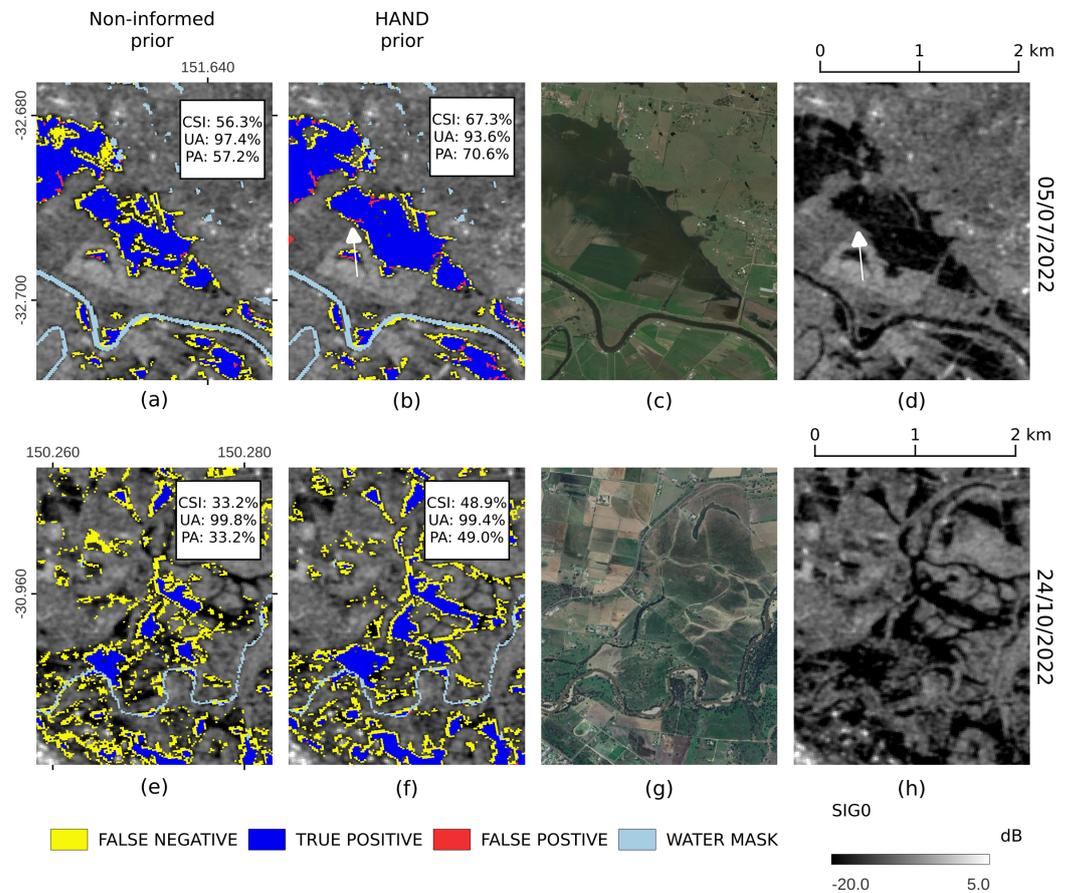


Figure 7. Confusion map of a portion of the New South Wales, Australia study sites. Top row: Confusion maps for the 05/07/2022 (Australia 1) flood event overlaid on SIG0 backscatter intensity at VV polarization for non-informed prior case (a) and HAND prior case (b); Google satellite map (c) and SIG0 backscatter intensity at VV polarization (d). Bottom row: Confusion maps for the 24/10/2022 (Australia 2) flood event overlaid on SIG0 backscatter intensity at VV polarization for non-informed prior case (e) and HAND prior case (f); Google satellite map (g) and SIG0 backscatter intensity at VV polarization (h).

4.2.4. Scotland

The Scotland test case shown in Figure 8 shows false negative issues around the border areas (white arrows) and masking of dark SAR backscatter pixels at higher elevation (green arrow).

Similar to other test sites, improvements along the flood edges are visible when comparing the non-informed prior case (a) to the HAND prior case (b). These edges or transition zones may contain mixed pixels [43] and complex scattering mechanisms [50] that cause a lesser decrease in the SAR (VV polarization) backscatter, which the original algorithm [23] has issues with and which the HAND priors rectify. Lastly, low-backscatter pixels masked by the HAND mask in the non-informed prior case (b) are labeled as non-flood in the HAND prior case (a).

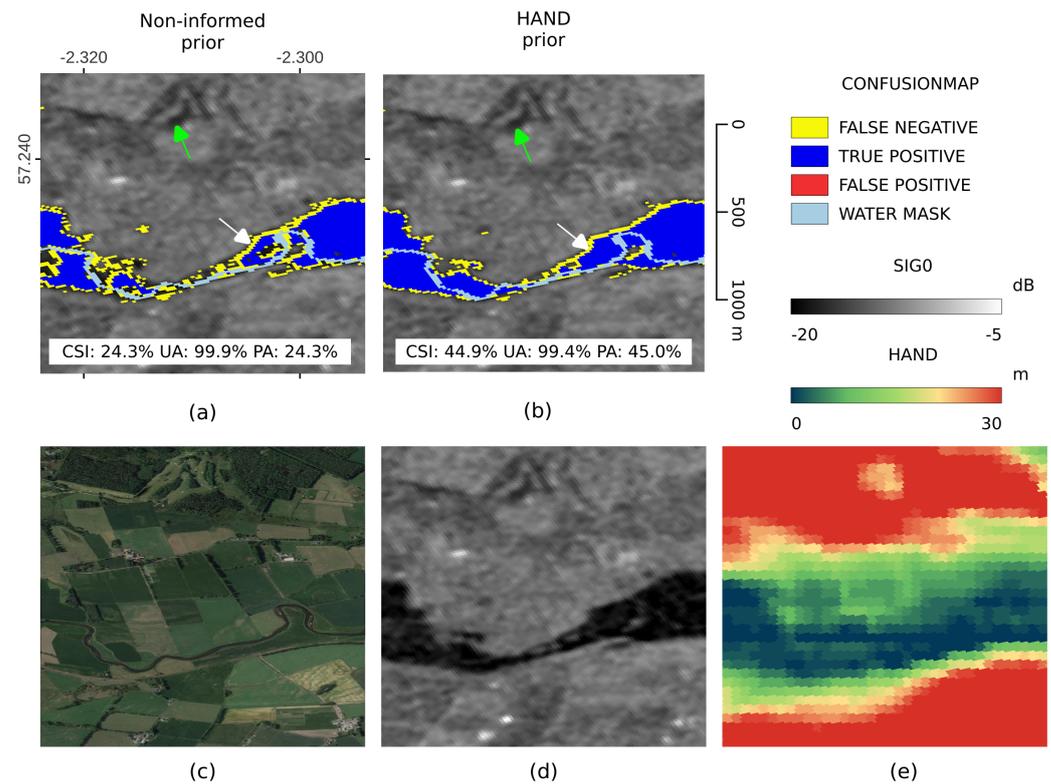


Figure 8. Confusion map of a portion of the Scotland study site. Top row: non-informed confusion maps for prior case (a) and HAND prior case (b). Bottom row: True color Google satellite map (c), SIG0 backscatter intensity at VV polarization (d), and HAND index map (e).

4.3. No-Flood Conditions

Table 2 shows the FPR calculated from the exemplary non-flooded images. The HAND column shows the FPR of flood maps using the HAND prior probability function, while the No Prior column shows the FPR of the maps with non-informed priors. It can be seen that the Valencia, Spain test site incurs both the largest FPR nominally for both cases and the most significant increase between the two. At the same time, minimal FPR was computed for Suriname. All study sites showed a small increase in FPR with the HAND-based prior, all below 1%.

Table 2. False Positive Rates for No-Flood Cases.

Location	No Prior	HAND Prior	Difference
Spain	1.50%	2.43%	0.92%
Suriname	0.00%	0.00%	0.00%
Australia 1	0.03%	0.12%	0.09%
Australia 2	0.07%	0.66%	0.59%
Belize	0.04%	0.20%	0.16%
Scotland	0.14%	0.14%	0.00%
average	0.30%	0.59%	0.29%

To qualitatively describe the performance of the HAND prior case versus the non-informed prior case in no-flood scenarios, we present the case with the highest FPR (Spain study site), shown in Figure 9. The zoomed-in area shown is located east of the Alarcon reservoir. It can be observed that the false positives cover (1) reservoir areas that are not normally inundated (black arrows) and (2) low-backscatter areas covering agricultural fields (white arrows). In the former, agricultural fields do not conform with the predicted seasonal backscatter response (see difference between panel d and b), leading to over-estimation—a known issue with the TU Wien algorithm [23]. At the same time, the latter is

a similar case and a common issue in EO flood mapping. Both issues appear to be slightly exacerbated by the HAND prior.

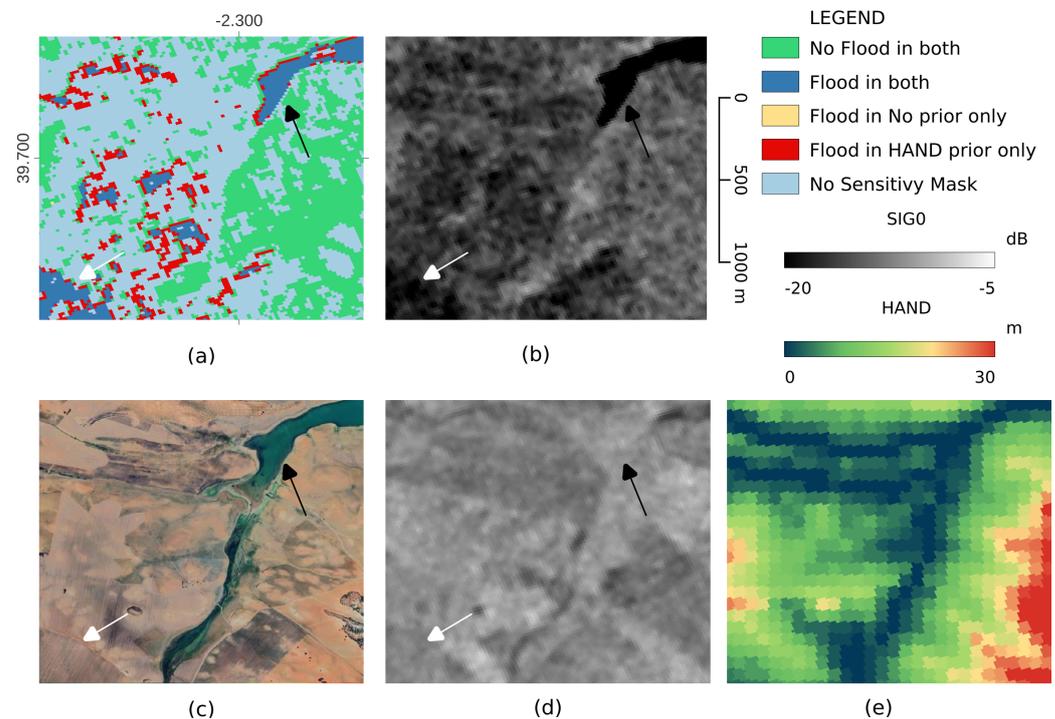


Figure 9. Confusion map of a non-flooded scenario in a portion of the Spain study site. Top row: difference map between the non-informed prior case and HAND prior case (a). SIG0 backscatter intensity at VV polarization on 2023-03-21 (b). Bottom row: true color Google satellite map (c), day-of-year estimated SIG0 backscatter intensity at VV polarization from the harmonic model (d), and HAND index map (e).

5. Summary and Conclusions

Our results demonstrate a noticeable improvement in the TU Wien flood mapping algorithm by applying a HAND-based prior probability function compared to the baseline non-informed prior. We introduced an exponential function and estimated globally applicable parameters to produce the HAND-based priors. We showed its performance on flooded and non-flooded cases in six study sites.

Concerning the HAND prior probability function, we have not found an optimum for its parameters, as the observed improvement in CSI and PA comes at the cost of UA. Thus, it is prudent to select a conservative estimate for the HAND prior probability function parameters that does not severely impact UA.

While empirically derived, the midpoint at 20m agrees with the assumption that this value should be within the usual range of HAND threshold values. On the other hand, lower steepness values proved to be useful, with 10m working well with the midpoints tested. Further parameter optimization could still improve flood mapping with HAND-based priors. However, given the close responses of the function to changes in parameters, we find the estimated parameters already suitable.

The HAND prior probability function introduced and tested here showed a promising performance. Applying the HAND-based priors decreases false negatives at the expense of a slight increase in false positives. In this regard, we observed less improvement in relatively flat areas than in areas with rolling terrain and low-lying areas. At the same time, we observed instances of similar masking effects when using the HAND prior probability function, thus removing the dependence on HAND masking.

In terms of reducing false negatives, flooded areas with a lesser decrease in backscatter intensities benefit from the HAND prior probabilities. The most commonly observed

occurrences of such areas are (1) floods in sparsely vegetated areas and (2) flood boundary or transition regions.

On the other hand, added false positive areas are typically found in low-lying areas with a minimal adverse effect of not masking at higher HAND values. Noting that the CEMS reference flood maps used were also delineated from the same Sentinel-1 images, we observed that some labeled false positives from the HAND prior test cases are most likely true positives that the CEMS rapid mapping method misclassified. On this point, we recommend further testing with independently sourced reference data.

For the no-flood scenarios, a slight increase in the false positive rates was observed for all six study sites tested. This test showed a reasonable performance, with no more than a 1% increase in FPR rates. We observe that the HAND prior slightly exacerbates existing issues with deviations from the expected seasonal backscatter response. Nevertheless, it should be pointed out that no extreme events (very dry or wet conditions) were captured in the six sites tested. As certain extreme events result in low-backscatter signals that lead to wholesale false positives, testing the performance of the HAND prior probabilities in such conditions is recommended.

To conclude, our flood mapping with HAND-based priors demonstrated improvements by decreasing false negatives at low HAND values and preventing false positives at high HAND values. The latter implies that we removed the need for an independent pre- or post-processing HAND mask. However, the improved algorithm has drawbacks: a slight increase in false positive rates and noted limitations for densely vegetated areas. We showed the suitability of applying a single parameterization to the six test sites, suggesting the feasible application of such priors to the TU Wien flood mapping algorithm at a global scale. With its simple formulation and ubiquitous input, this *prior* formulation could potentially benefit other Bayesian or probabilistic flood mapping workflows.

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Abbreviations

The following abbreviations are used in this manuscript:

CEMS	Copernicus Emergency Management Service
CSI	Critical Success Index
DEM	Digital Elevation Model

DOY	Day Of Year
EODC	Earth Observation Data Centre for Water Resource Monitoring
FPR	False Positive Rate
GFM	Global Flood Monitoring
GRD	Ground Range Detected
HAND	Height Above Nearest Drainage
PA	Producer's Accuracy
PLIA	Projected Local Incidence Angle θ
UA	User's Accuracy
PDF	Probability Distribution Function
NRT	Near-Real-Time
SAR	Synthetic Aperture Radar
SIG0	Sigma Nought backscatter coefficient σ_0

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